

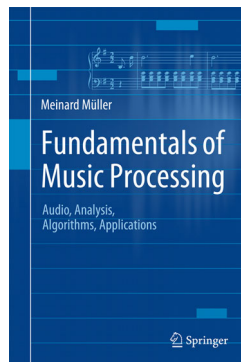
Lecture
Music Processing

Music Structure Analysis

Meinard Müller

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Book: Fundamentals of Music Processing



Meinard Müller
 Fundamentals of Music Processing
 Audio, Analysis, Algorithms, Applications
 483 p., 249 illus., hardcover
 ISBN: 978-3-319-21944-8
 Springer, 2015

Accompanying website:
www.music-processing.de

Book: Fundamentals of Music Processing

Chapter	Music Processing Scenario
1	Music Representations
2	Fourier Analysis of Signals
3	Music Synchronization
4	Music Structure Analysis
5	Chord Recognition
6	Tempo and Beat Tracking
7	Content-Based Audio Retrieval
8	Musically Informed Audio Decomposition

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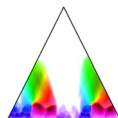
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Chapter 4: Music Structure Analysis

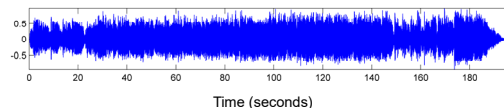
- 4.1 General Principles
- 4.2 Self-Similarity Matrices
- 4.3 Audio Thumbnailing
- 4.4 Novelty-Based Segmentation
- 4.5 Evaluation
- 4.6 Further Notes



In Chapter 4, we address a central and well-researched area within MIR known as music structure analysis. Given a music recording, the objective is to identify important structural elements and to temporally segment the recording according to these elements. Within this scenario, we discuss fundamental segmentation principles based on repetitions, homogeneity, and novelty—principles that also apply to other types of multimedia beyond music. As an important technical tool, we study in detail the concept of self-similarity matrices and discuss their structural properties. Finally, we briefly touch the topic of evaluation, introducing the notions of precision, recall, and F-measure.

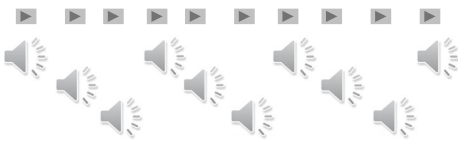
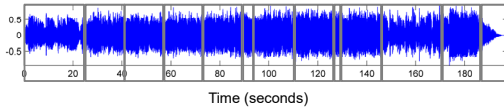
Music Structure Analysis

Example: Zager & Evans "In The Year 2525"



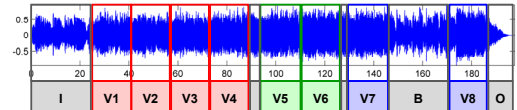
Music Structure Analysis

Example: Zager & Evans "In The Year 2525"



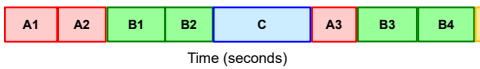
Music Structure Analysis

Example: Zager & Evans "In The Year 2525"



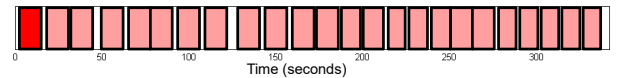
Music Structure Analysis

Example: Brahms Hungarian Dance No. 5 (Ormandy)



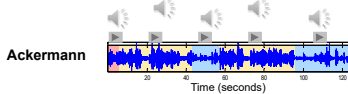
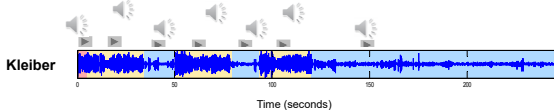
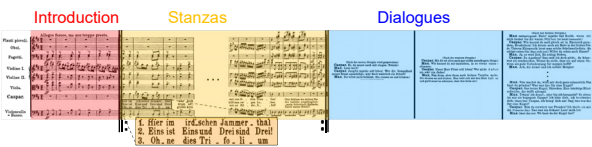
Music Structure Analysis

Example: Folk Song Field Recording (Nederlandse Liederbank)



Music Structure Analysis

Example: Weber, Song (No. 4) from "Der Freischütz"



Music Structure Analysis

General goal: Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

Examples:

- Stanzas of a folk song
- Intro, verse, chorus, bridge, outro sections of a pop song
- Exposition, development, recapitulation, coda of a sonata
- Musical form ABACADA ... of a rondo

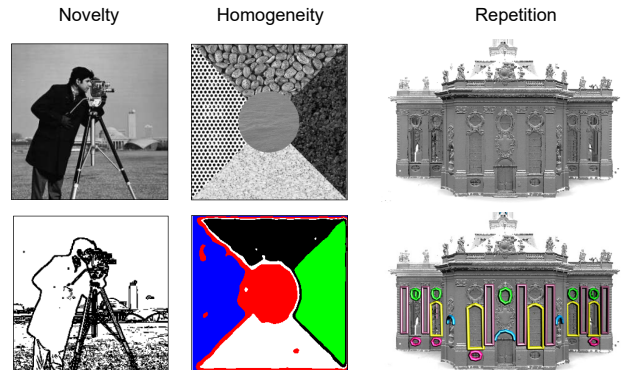
Music Structure Analysis

General goal: Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

Challenge: There are many different principles for creating relationships that form the basis for the musical structure.

- **Homogeneity:** Consistency in tempo, instrumentation, key, ...
- **Novelty:** Sudden changes, surprising elements ...
- **Repetition:** Repeating themes, motives, rhythmic patterns,...

Music Structure Analysis



Overview

- **Introduction**
 - Feature Representations
 - Self-Similarity Matrices
 - Audio Thumbnailing
 - Novelty-based Segmentation
- Thanks:**
- Clausen, Ewert, Kurth, Grohganz, ...
 - Dannenberg, Goto
 - Grosche, Jiang
 - Paulus, Klapuri
 - Peeters, Kaiser, ...
 - Serra, Gómez, ...
 - Smith, Fujinaga, ...
 - Wiering, ...
 - Wand, Sunkel, Jansen
 - ...

Overview

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Feature Representation

General goal: Convert an audio recording into a mid-level representation that captures certain musical properties while suppressing other properties.

- Timbre / Instrumentation
- Tempo / Rhythm
- Pitch / Harmony

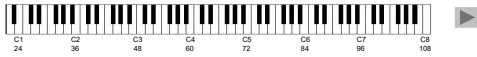
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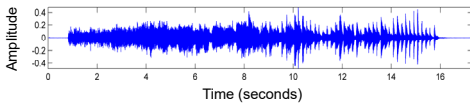
- Timbre / Instrumentation
- Tempo / Rhythm
- **Pitch / Harmony**

Feature Representation

Example: Chromatic scale



Waveform

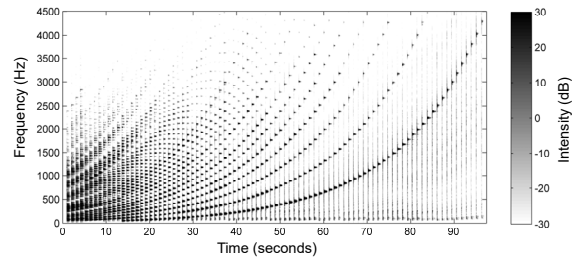


Feature Representation

Example: Chromatic scale



Spectrogram

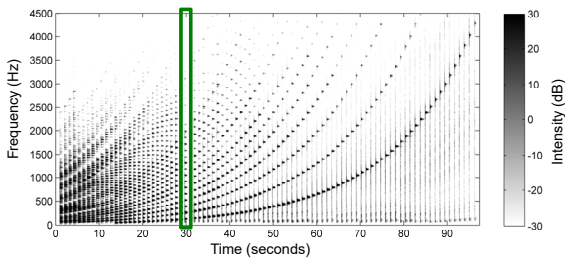


Feature Representation

Example: Chromatic scale

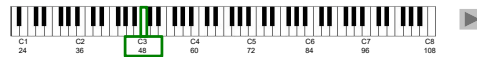


Spectrogram

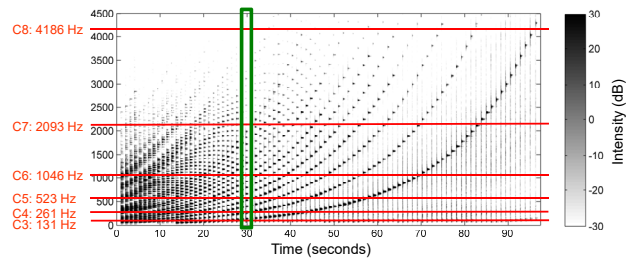


Feature Representation

Example: Chromatic scale



Spectrogram

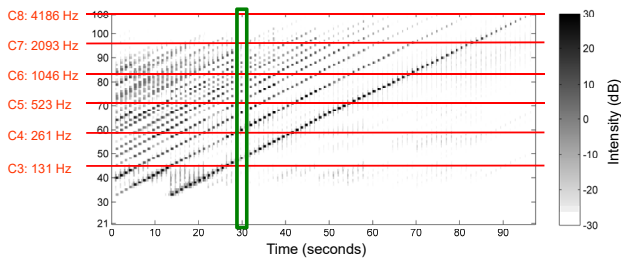


Feature Representation

Example: Chromatic scale



Log-frequency spectrogram

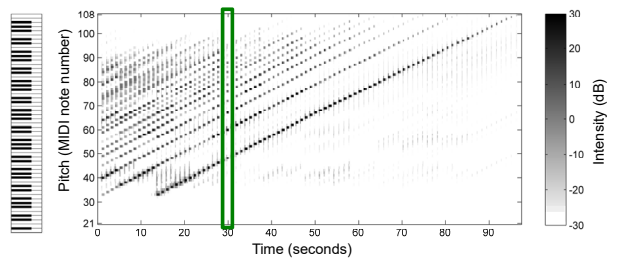


Feature Representation

Example: Chromatic scale



Log-frequency spectrogram

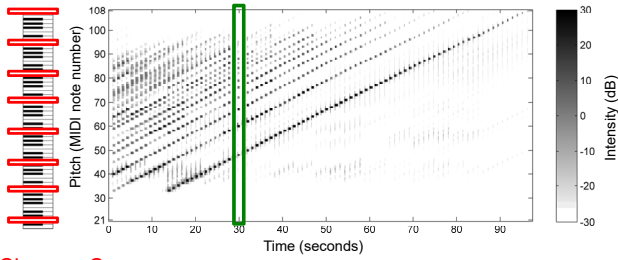


Feature Representation

Example: Chromatic scale



Log-frequency spectrogram



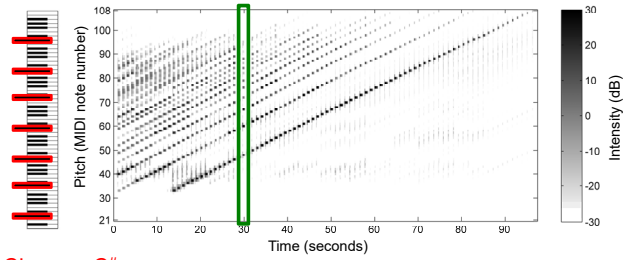
Chroma C

Feature Representation

Example: Chromatic scale



Log-frequency spectrogram



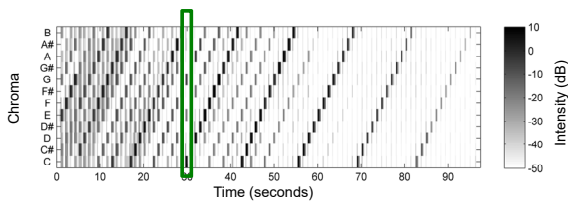
Chroma C#

Feature Representation

Example: Chromatic scale

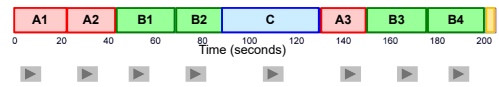
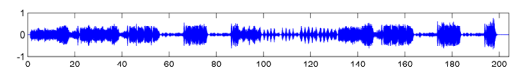


Chroma representation



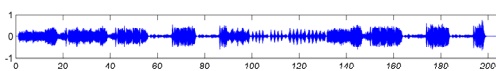
Feature Representation

Example: Brahms Hungarian Dance No. 5 (Ormandy)



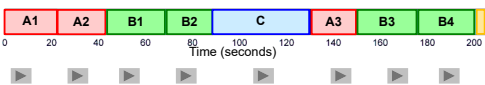
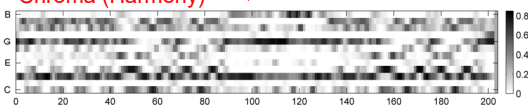
Feature Representation

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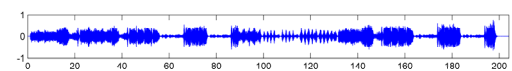
Chroma (Harmony)

Feature extraction



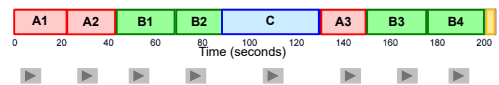
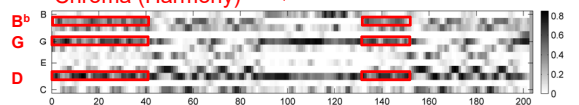
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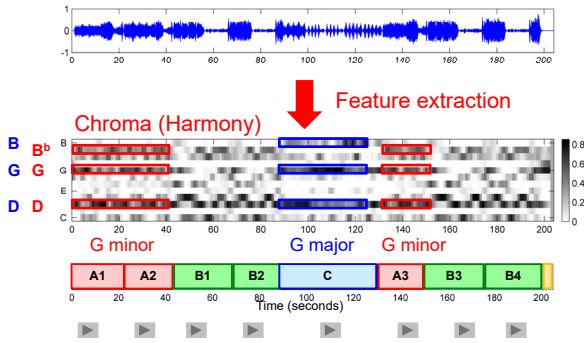
Chroma (Harmony)

Feature extraction



Feature Representation

Example: Brahms Hungarian Dance No. 5 (Ormandy)



Overview

- Introduction
- Feature Representations
- Self-Similarity Matrices
- Audio Thumbnailing
- Novelty-based Segmentation

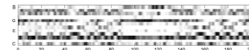
Self-Similarity Matrix (SSM)

General idea: Compare each element of the feature sequence with each other element of the feature sequence based on a suitable similarity measure.

→ Quadratic self-similarity matrix

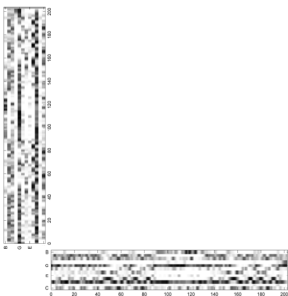
Self-Similarity Matrix (SSM)

Example: Brahms Hungarian Dance No. 5 (Ormandy)



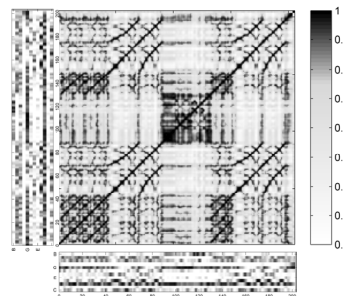
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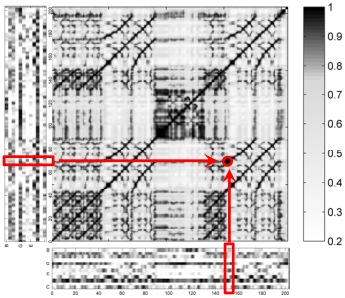
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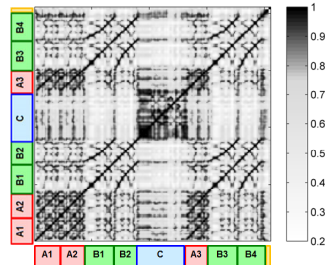
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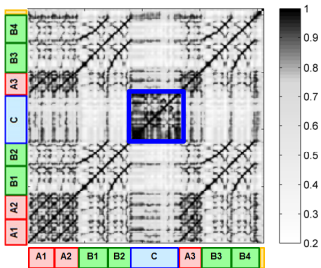
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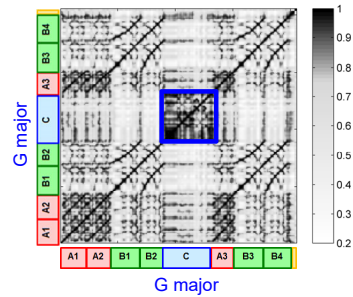
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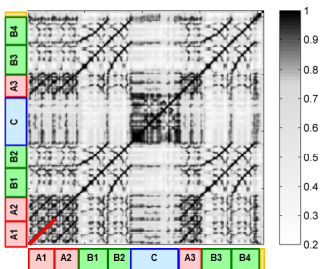
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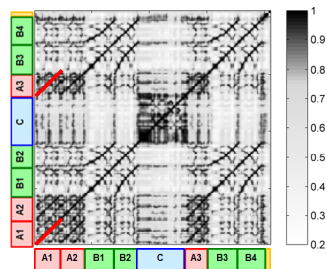
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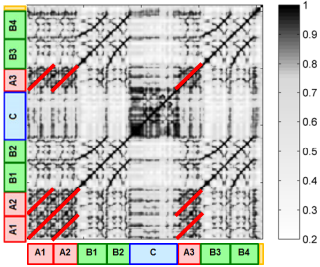
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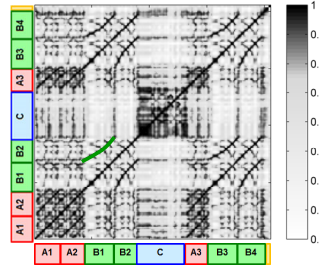
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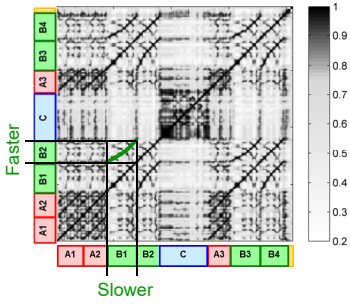
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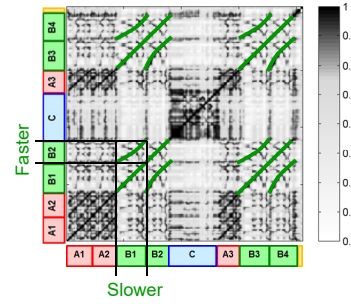
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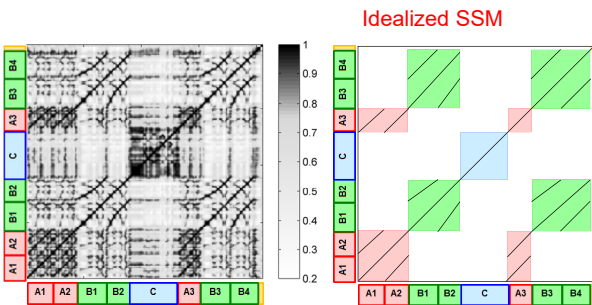
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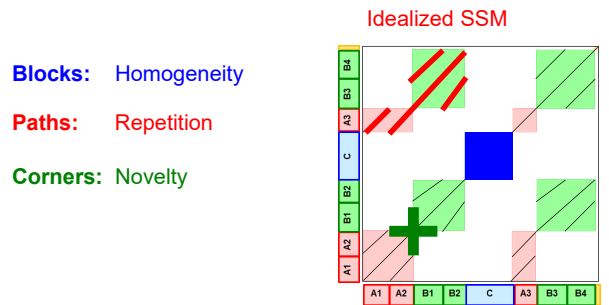
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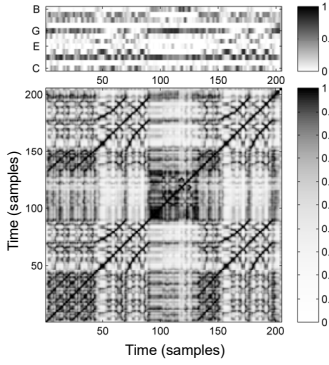


Blocks: Homogeneity

Paths: Repetition

Corners: Novelty

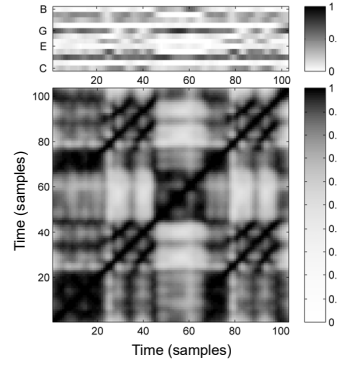
SSM Enhancement



Block Enhancement

- Feature smoothing
- Coarsening

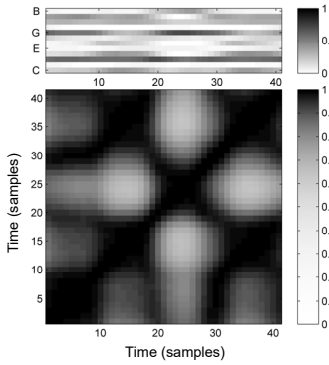
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Block Enhancement

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SSM Enhancement



Block Enhancement

- Feature smoothing
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SSM Enhancement

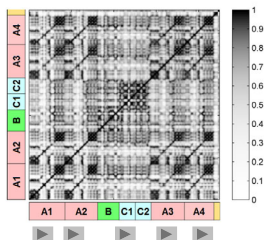
Challenge: Presence of musical variations

- Fragmented paths and gaps
- Paths of poor quality
- Regions of constant (high) similarity
- Curved paths

Idea: Enhancement of path structure

SSM Enhancement

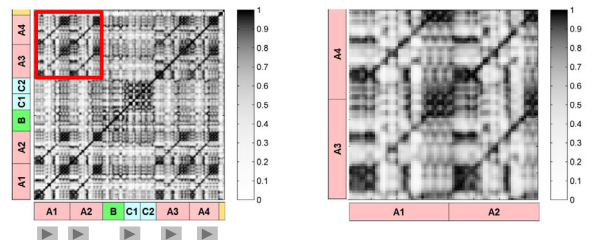
Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



SSM

SSM Enhancement

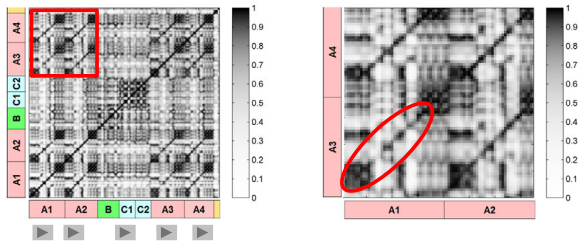
Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



SSM

SSM Enhancement

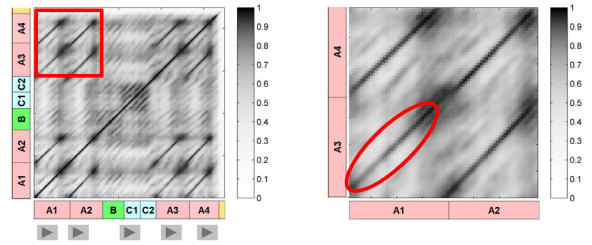
Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



SSM

SSM Enhancement

Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



Enhanced SSM

Filtering along main diagonal

SSM Enhancement

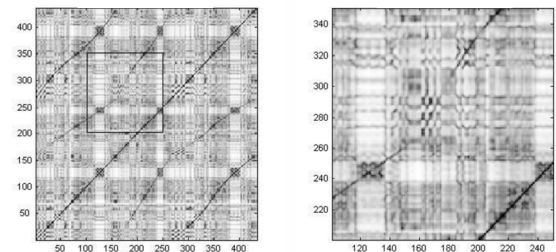
Idea: Usage of contextual information (Foote 1999)

$$S_L(n, m) := \frac{1}{L} \sum_{\ell=0}^{L-1} S(n + \ell, m + \ell)$$

- Comparison of entire sequences
- L = length of sequences
- S_L = enhanced SSM

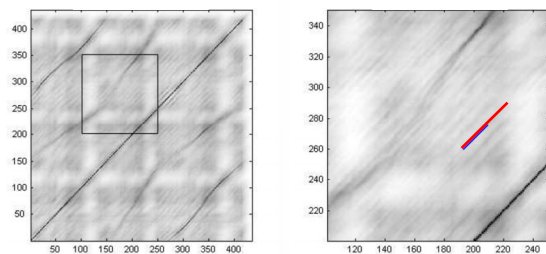
↪ smoothing effect

SSM Enhancement



SSM S

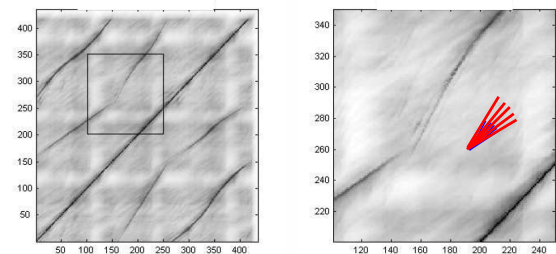
SSM Enhancement



Enhanced SSM S_L with $L = 20$

Filtering along main diagonal

SSM Enhancement



Enhanced SSM $S_{L,\Theta}$ with $L = 20$

Filtering along 8 different directions and minimizing

SSM Enhancement

Idea: Smoothing along various directions and minimizing over all directions

$$\Theta = \{0.66, 0.81, 1.00, 1.22, 1.50\}$$

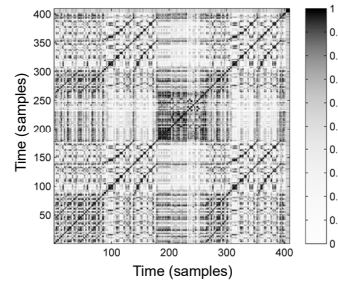
$$S_{L,\theta}(n,m) := \frac{1}{L} \sum_{\ell=0}^{L-1} S(n+\ell, m + [\ell \cdot \theta])$$

$$S_{L,\Theta}(n,m) := \max_{\theta \in \Theta} S_{L,\theta}(n,m)$$

↪ Tempo changes of -50 to +50 percent

SSM Enhancement

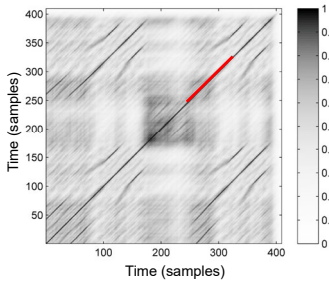
Path Enhancement



SSM Enhancement

Path Enhancement

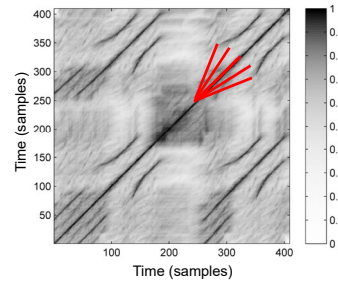
- Diagonal smoothing



SSM Enhancement

Path Enhancement

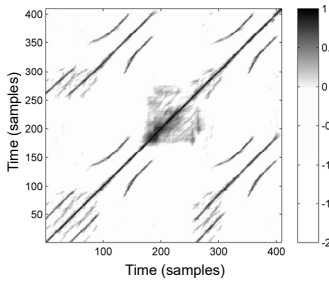
- Diagonal smoothing
- Multiple filtering



SSM Enhancement

Path Enhancement

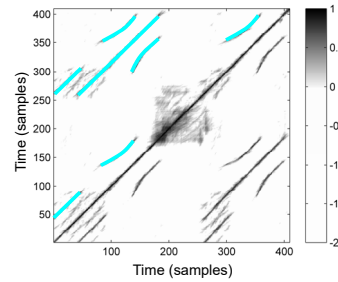
- Diagonal smoothing
- Multiple filtering
- Thresholding (relative)
- Scaling & penalty



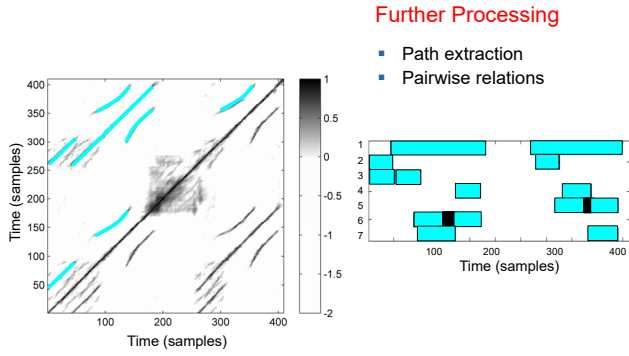
SSM Enhancement

Further Processing

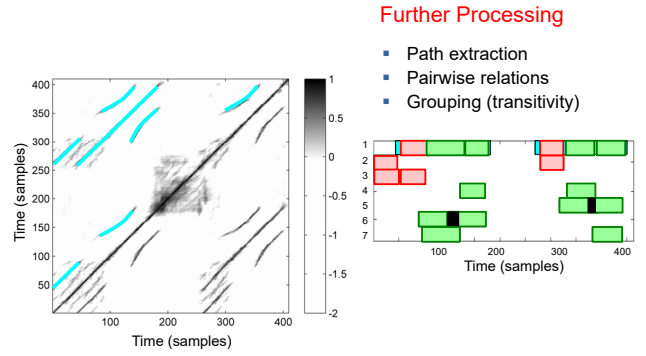
- Path extraction



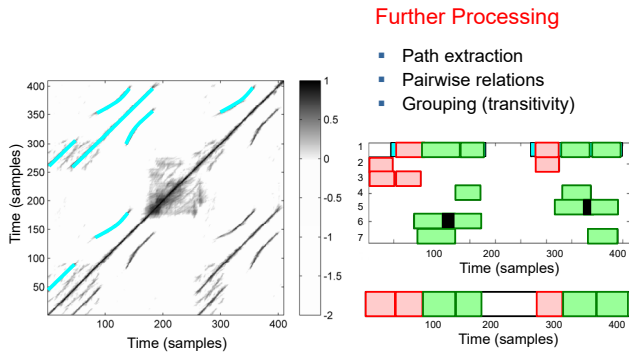
SSM Enhancement



SSM Enhancement

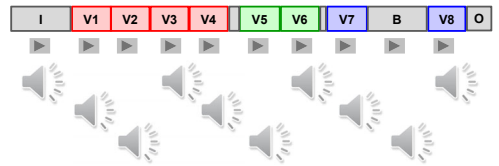


SSM Enhancement



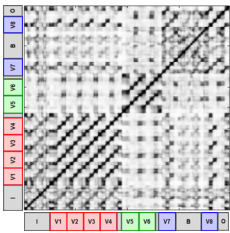
SSM Enhancement

Example: Zager & Evans "In The Year 2525"



SSM Enhancement

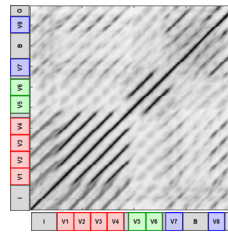
Example: Zager & Evans "In The Year 2525"



SSM Enhancement

Example: Zager & Evans "In The Year 2525"

Missing relations because of transposed sections



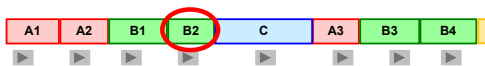
Audio Thumbnailing

General goal: Determine the most representative section ("Thumbnail") of a given music recording.

Example: Zager & Evans "In The Year 2525"



Example: Brahms Hungarian Dance No. 5 (Ormandy)



Thumbnail is often assumed to be the most repetitive segment

Audio Thumbnailing

Two steps

1. Path extraction

Both steps are problematic!

- Paths of poor quality (fragmented, gaps)
- Block-like structures
- Curved paths

2. Grouping

- Noisy relations (missing, distorted, overlapping)
- Transitivity computation difficult

Main idea: Do both, path extraction and grouping, jointly

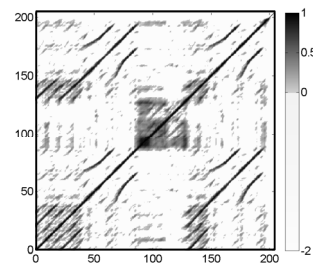
- One optimization scheme for both steps
- Stabilizing effect
- Efficient

Audio Thumbnailing

Main idea: Do both path extraction and grouping jointly

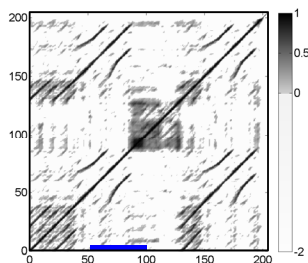
- For each audio **segment** we define a **fitness** value
- This fitness value expresses "how well" the segment explains the entire audio recording
- The segment with the highest fitness value is considered to be the **thumbnail**
- As main technical concept we introduce the notion of a **path family**

Fitness Measure



Enhanced SSM

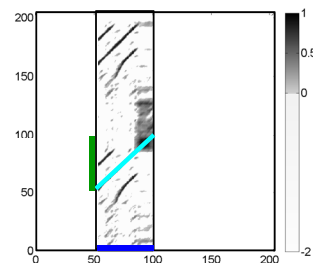
Fitness Measure



Path over segment

- Consider a fixed **segment**

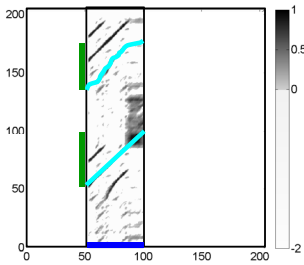
Fitness Measure



Path over segment

- Consider a fixed **segment**
- **Path** over **segment**
- **Induced segment**
- Score is high

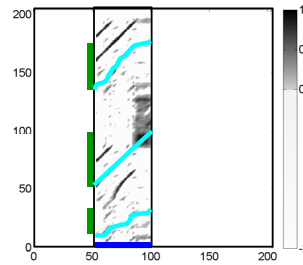
Fitness Measure



Path over segment

- Consider a fixed **segment**
- Path** over **segment**
- Induced segment**
- Score is high
- A second path** over **segment**
- Induced segment**
- Score is not so high

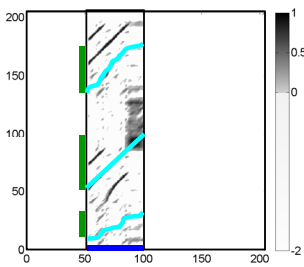
Fitness Measure



Path over segment

- Consider a fixed **segment**
- Path** over **segment**
- Induced segment**
- Score is high
- A second path** over **segment**
- Induced segment**
- Score is not so high
- A third path** over **segment**
- Induced segment**
- Score is very low

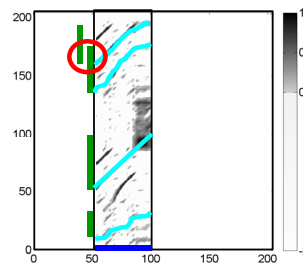
Fitness Measure



Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

Fitness Measure

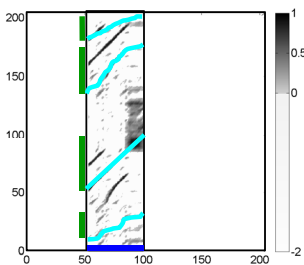


Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is **not** a path family!

Fitness Measure



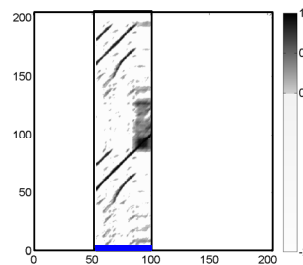
Path family

- Consider a fixed **segment**
- A path family over a **segment** is a family of paths such that the **induced segments** do **not overlap**.

This is a path family!

(Even though not a good one)

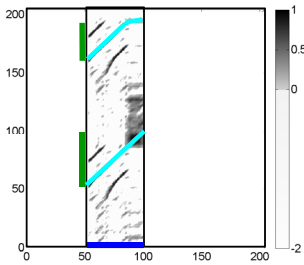
Fitness Measure



Optimal path family

- Consider a fixed **segment**

Fitness Measure

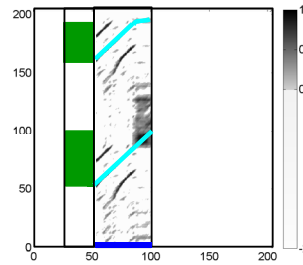


Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:
 $\text{Score}(\text{segment})$

Note: This optimal path family can be computed using dynamic programming.

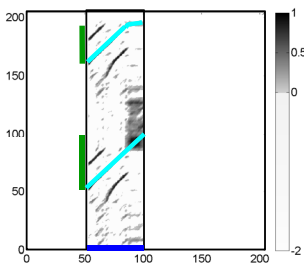
Fitness Measure



Optimal path family

- Consider a fixed **segment**
- Consider over the **segment** the **optimal path family**, i.e., the path family having maximal overall score.
- Call this value:
 $\text{Score}(\text{segment})$
- Furthermore consider the amount covered by the **induced segments**.
- Call this value:
 $\text{Coverage}(\text{segment})$

Fitness Measure

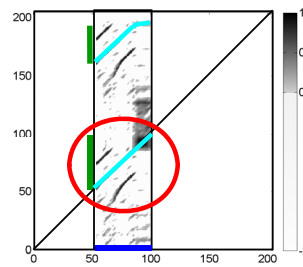


Fitness

- Consider a fixed **segment**

$P := \text{Score}(\text{segment})$
 $R := \text{Coverage}(\text{segment})$

Fitness Measure

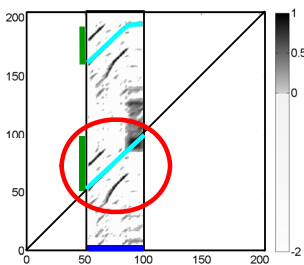


Fitness

- Consider a fixed **segment**
- Self-explanation are trivial!**

$P := \text{Score}(\text{segment})$
 $R := \text{Coverage}(\text{segment})$

Fitness Measure

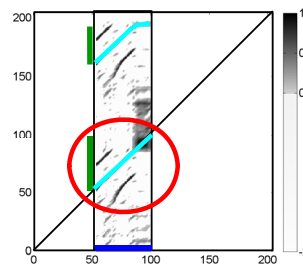


Fitness

- Consider a fixed **segment**
- Self-explanation are trivial!**
- Subtract length of **segment**

$P := \text{Score}(\text{segment}) - \text{length}(\text{segment})$
 $R := \text{Coverage}(\text{segment}) - \text{length}(\text{segment})$

Fitness Measure

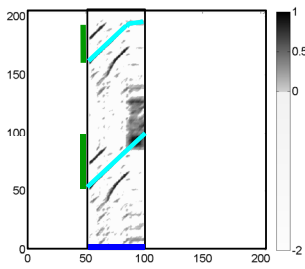


Fitness

- Consider a fixed **segment**
- Self-explanation are trivial!**
- Subtract length of **segment**
- Normalization

$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$
 $R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$

Fitness Measure



Fitness

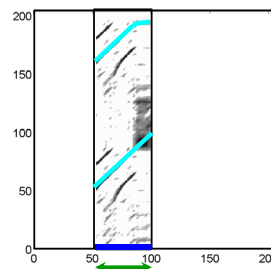
- Consider a fixed segment

$$F := 2 \cdot P \cdot R / (P + R)$$

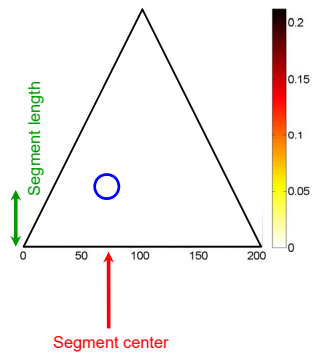
$$P := \text{Normalize}(\text{Score}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

$$R := \text{Normalize}(\text{Coverage}(\text{segment}) - \text{length}(\text{segment})) \in [0,1]$$

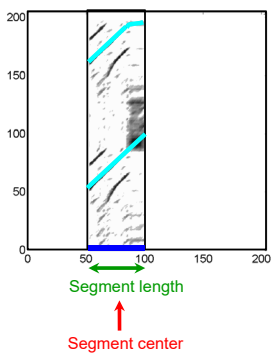
Thumbnail



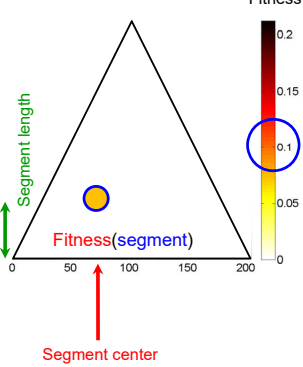
Fitness Scape Plot



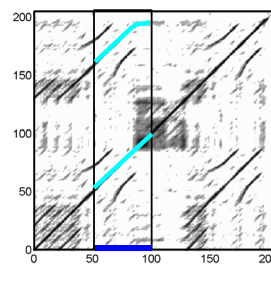
Thumbnail



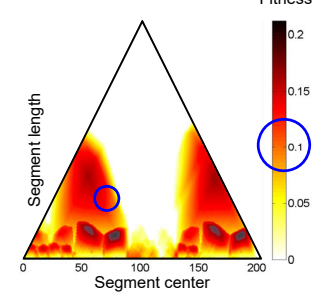
Fitness Scape Plot



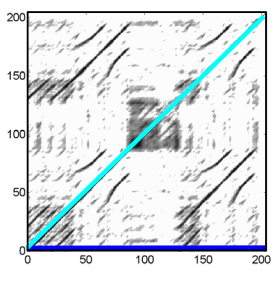
Thumbnail



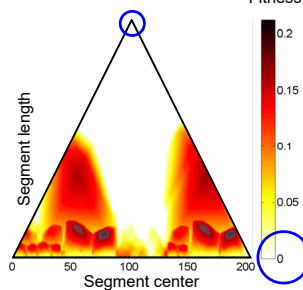
Fitness Scape Plot



Thumbnail

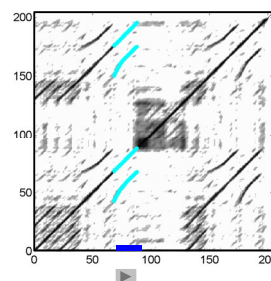


Fitness Scape Plot

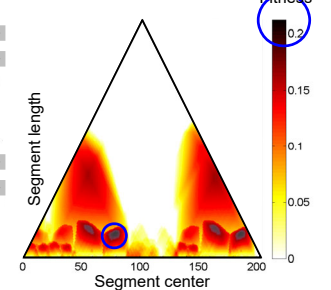


Note: Self-explanations are ignored → fitness is zero

Thumbnail

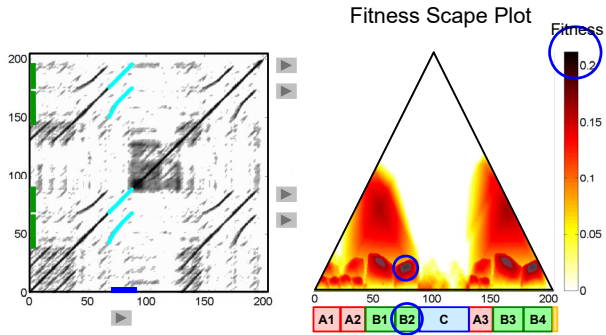


Fitness Scape Plot



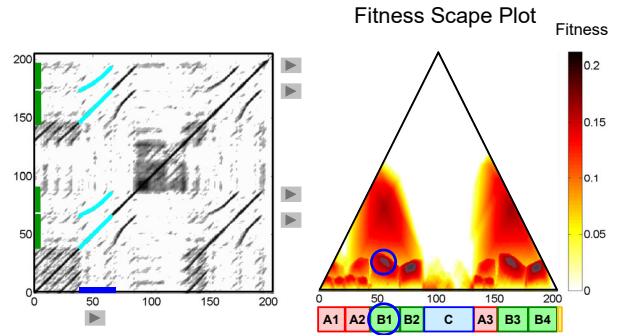
Thumbnail := segment having the highest fitness

Thumbnail



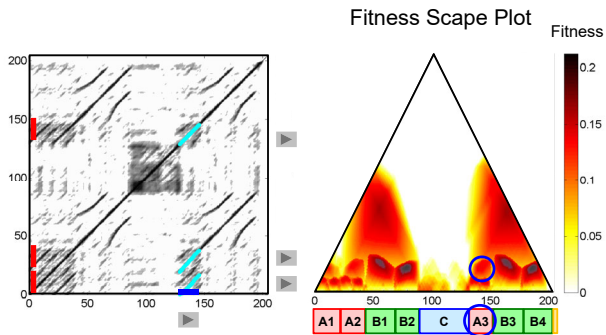
Example: Brahms Hungarian Dance No. 5 (Ormandy)

Thumbnail



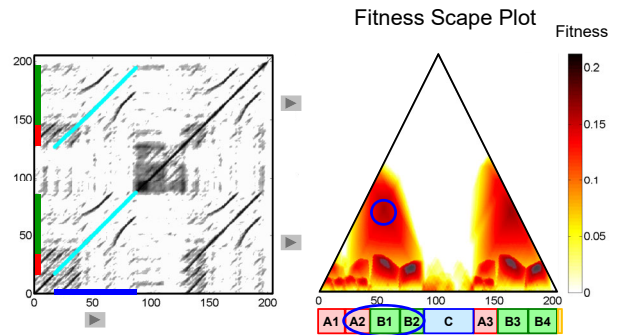
Example: Brahms Hungarian Dance No. 5 (Ormandy)

Thumbnail



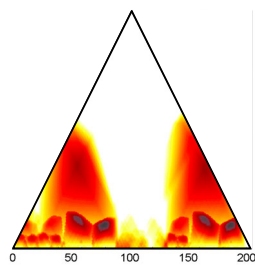
Example: Brahms Hungarian Dance No. 5 (Ormandy)

Thumbnail



Example: Brahms Hungarian Dance No. 5 (Ormandy)

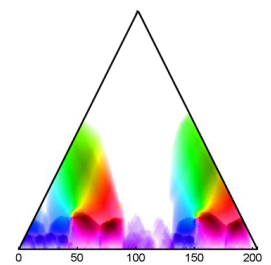
Scape Plot



Example: Brahms Hungarian Dance No. 5 (Ormandy)

Scape Plot

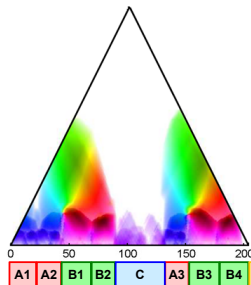
Coloring according to clustering result (grouping)



Example: Brahms Hungarian Dance No. 5 (Ormandy)

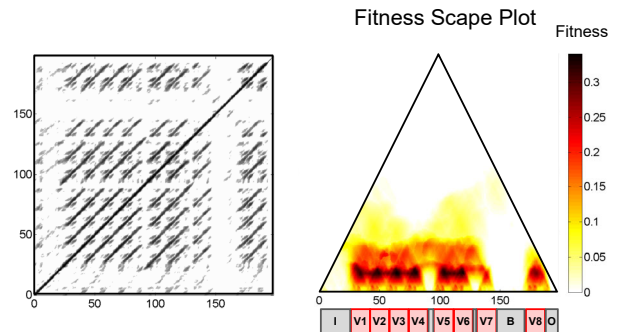
Scape Plot

Coloring according to clustering result (grouping)



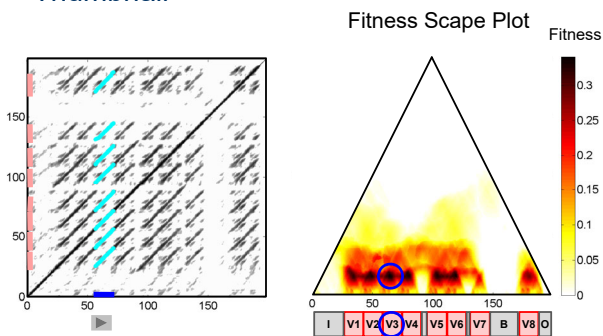
Example: Brahms Hungarian Dance No. 5 (Ormandy)

Thumbnail



Example: Zager & Evans "In The Year 2525"

Thumbnail



Example: Zager & Evans "In The Year 2525"

Overview

- Introduction
- Feature Representations
- Self-Similarity Matrices
- Audio Thumbling
- Novelty-based Segmentation

Thanks:

- Foote
- Serra, Grosche, Arcos
- Goto
- Tzanetakis, Cook

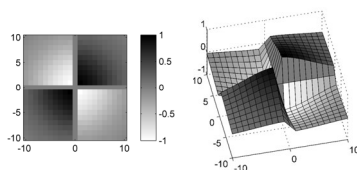
Novelty-based Segmentation

General goals:

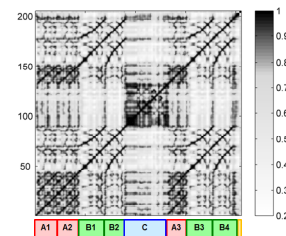
- Find instances where musical changes occur.
- Find transition between subsequent musical parts.

Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.



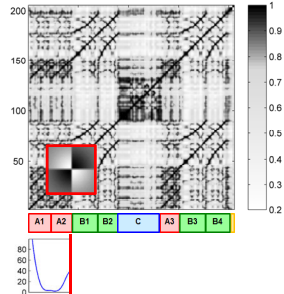
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

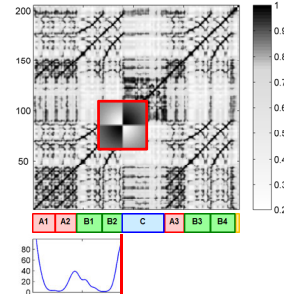
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

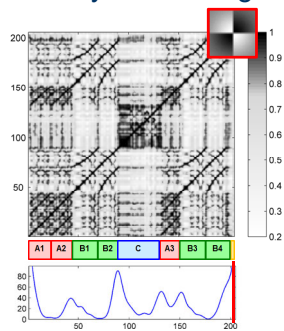
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

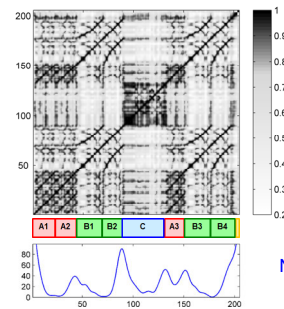
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty-based Segmentation



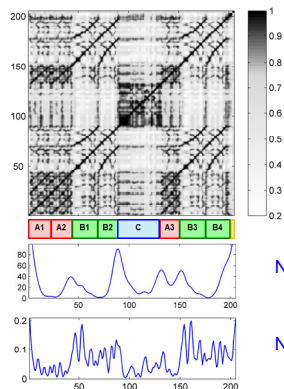
Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using



Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using



Novelty function using



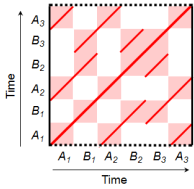
Novelty-based Segmentation

Idea:

- Find instances where **structural** changes occur.
- Combine **global** and **local** aspects within a unifying framework

Structure features

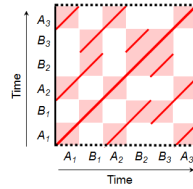
Novelty-based Segmentation



Structure features

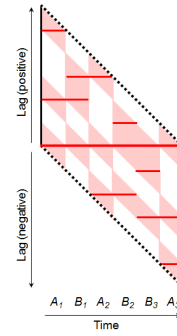
- Enhanced SSM

Novelty-based Segmentation

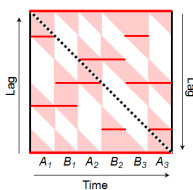
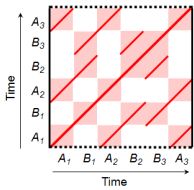


Structure features

- Enhanced SSM
- Time-lag SSM



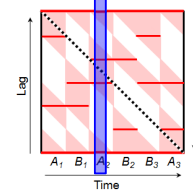
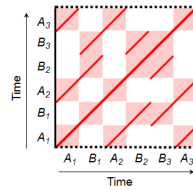
Novelty-based Segmentation



Structure features

- Enhanced SSM
- Time-lag SSM
- Cyclic time-lag SSM

Novelty-based Segmentation

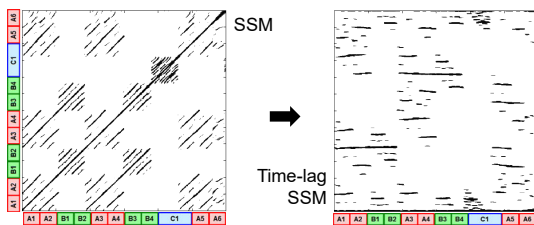


Structure features

- Enhanced SSM
- Time-lag SSM
- Cyclic time-lag SSM
- Columns as features

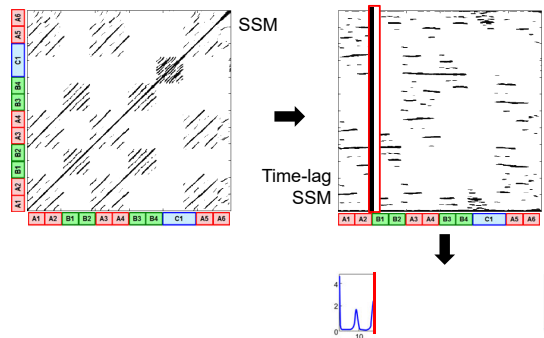
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



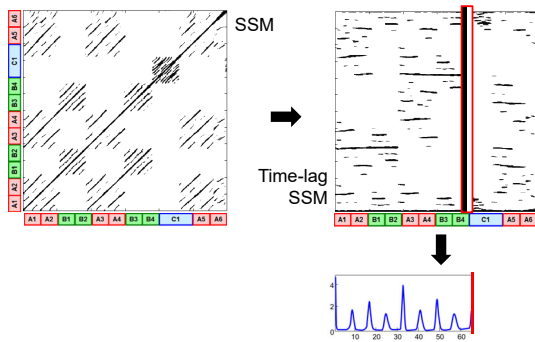
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



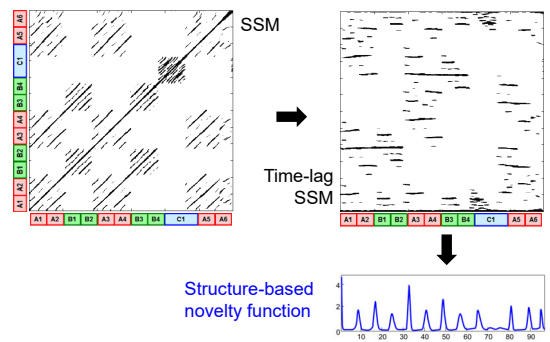
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



Novelty-based Segmentation

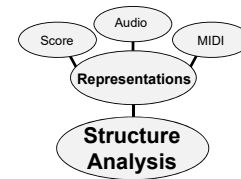
Example: Chopin Mazurka Op. 24, No. 1



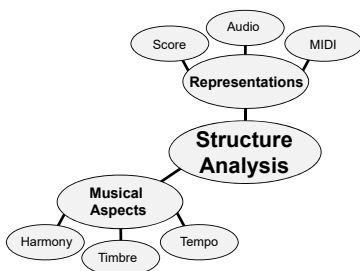
Conclusions

Structure Analysis

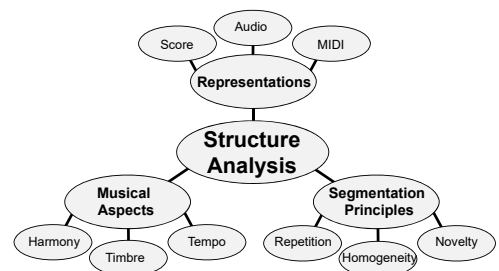
Conclusions



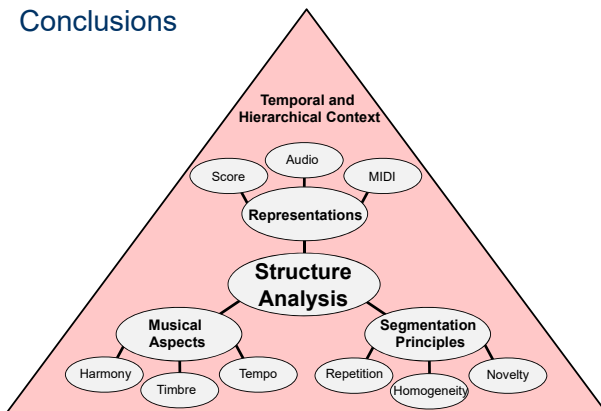
Conclusions



Conclusions

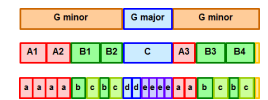
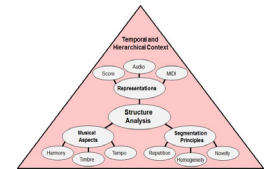


Conclusions



Conclusions

- Combined Approaches
- Hierarchical Approaches
- Evaluation
- Explaining Structure



- MIREX
- SALAMI-Project
- Smith, Chew

Links

- SM Toolbox (MATLAB)
<http://www.audiolabs-erlangen.de/resources/MIR/SMtoolbox/>
- MSFA: Music Structure Analysis Framework (Python)
<https://github.com/urinieto/msaf>
- SALAMI Annotation Data
<http://ddmal.music.mcgill.ca/research/salami/annotations>
- LibROSA (Python)
<https://librosa.github.io/librosa/>
- Evaluation: mir_eval (Python)
https://craffel.github.io/mir_eval/
- Deep Learning: Boundary Detection
Jan Schlüter (PhD thesis)