

Lecture **Music Processing**

Tempo and Beat Tracking

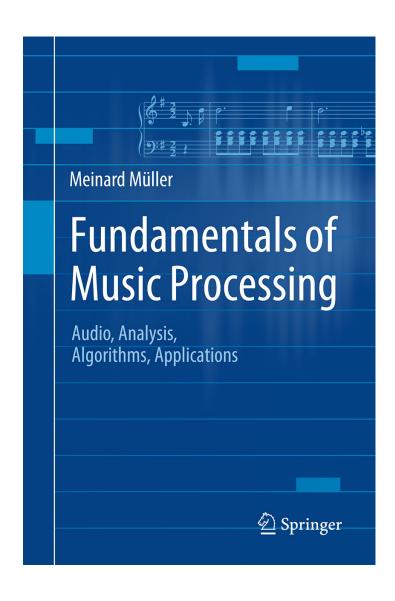
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Book: Fundamentals of Music Processing



Meinard Müller
Fundamentals of Music Processing
Audio, Analysis, Algorithms, Applications
483 p., 249 illus., hardcover
ISBN: 978-3-319-21944-8
Springer, 2015

Accompanying website: www.music-processing.de

Book: Fundamentals of Music Processing

Chapter		Music Processing Scenario
1		Music Represenations
2		Fourier Analysis of Signals
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6	1	Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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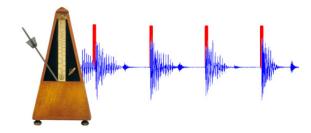
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Chapter 6: Tempo and Beat Tracking

- 6.1 Onset Detection
- 6.2 Tempo Analysis
- 6.3 Beat and Pulse Tracking
- 6.4 Further Notes



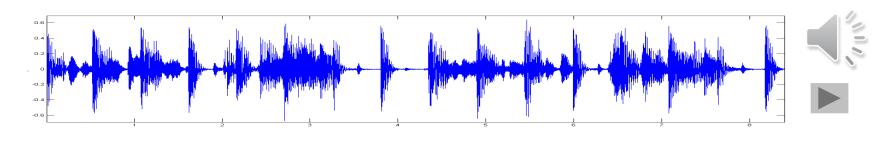
Tempo and beat are further fundamental properties of music. In Chapter 6, we introduce the basic ideas on how to extract tempo-related information from audio recordings. In this scenario, a first challenge is to locate note onset information—a task that requires methods for detecting changes in energy and spectral content. To derive tempo and beat information, note onset candidates are then analyzed with regard to quasiperiodic patterns. This leads us to the study of general methods for local periodicity analysis of time series.

Basic beat tracking task:

Given an audio recording of a piece of music, determine the periodic sequence of beat positions.

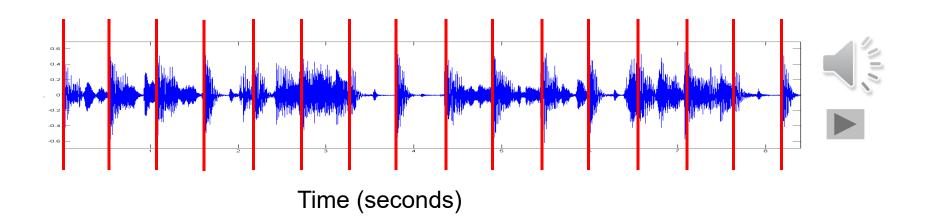
"Tapping the foot when listening to music"

Example: Queen – Another One Bites The Dust



Time (seconds)

Example: Queen – Another One Bites The Dust



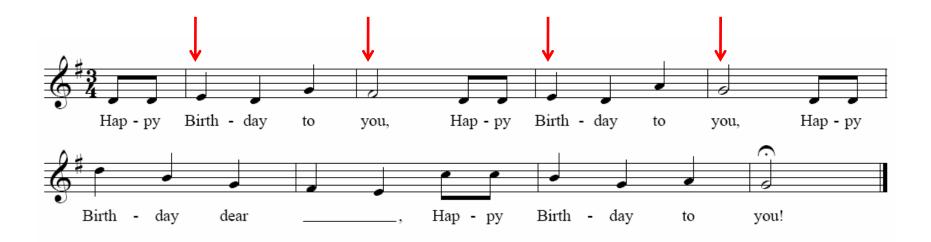






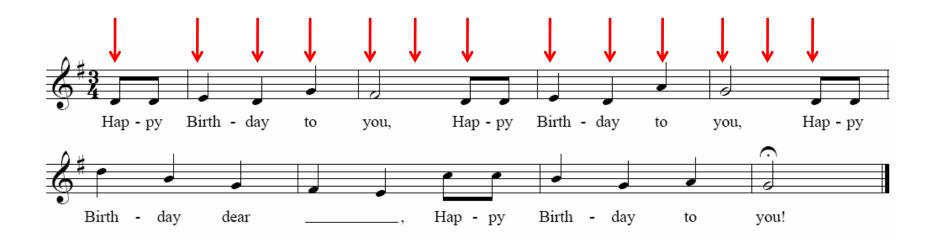
Example: Happy Birthday to you

Pulse level: Measure



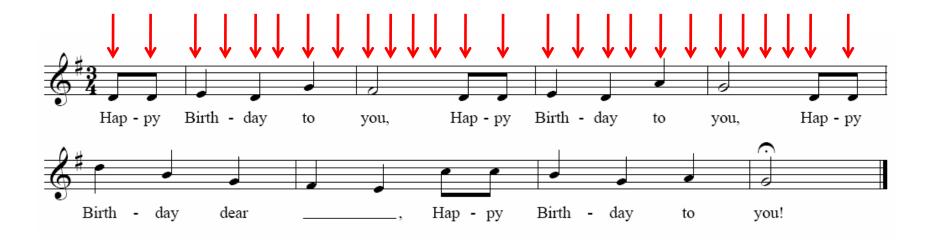
Example: Happy Birthday to you

Pulse level: Tactus (beat)



Example: Happy Birthday to you

Pulse level: Tatum (temporal atom)



Example: Chopin – Mazurka Op. 68-3

Pulse level: Quarter note

Tempo: ???













Example: Chopin – Mazurka Op. 68-3

Pulse level: Quarter note

Tempo: 50-200 BPM





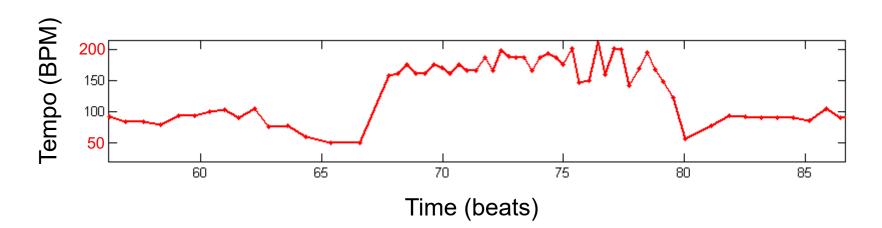








Tempo curve



Example: Borodin – String Quartet No. 2

Pulse level: Quarter note

Tempo: 120-140 BPM (roughly)

Beat tracker without any prior knowledge



Beat tracker with prior knowledge on rough tempo range



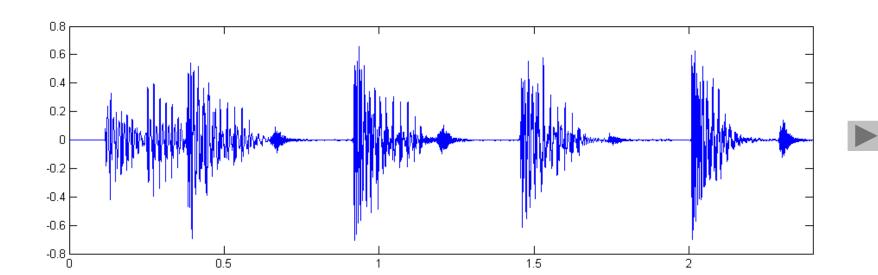


Challenges in beat tracking

- Pulse level often unclear
- Local/sudden tempo changes (e.g. rubato)
- Vague information
 (e.g., soft onsets, extracted onsets corrupt)
- Sparse information
 (often only note onsets are used)

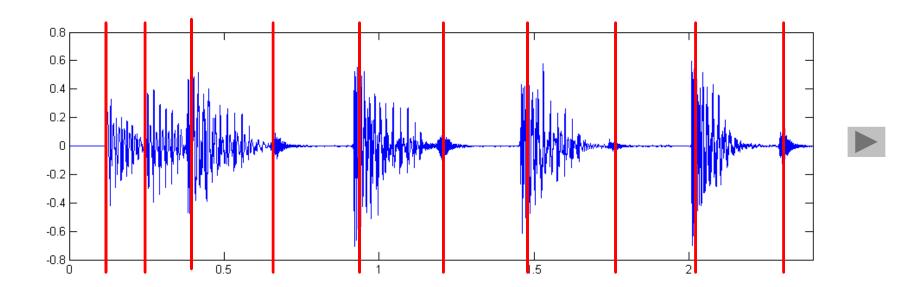
Tasks

- Onset detection
- Beat tracking
- Tempo estimation



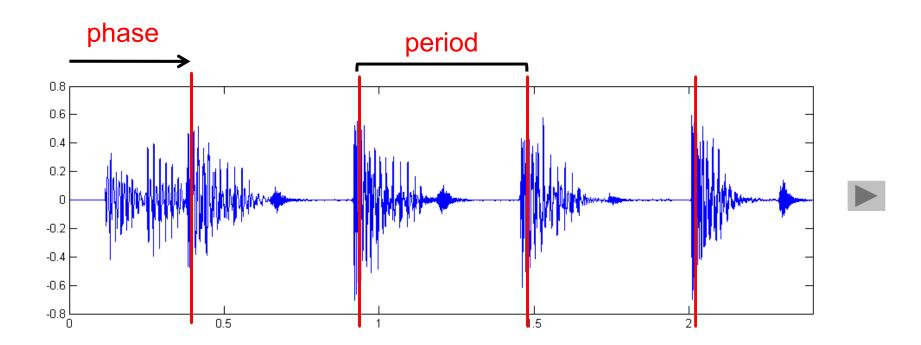
Tasks

- Onset detection
- Beat tracking
- Tempo estimation



Tasks

- Onset detection
- Beat tracking
- Tempo estimation

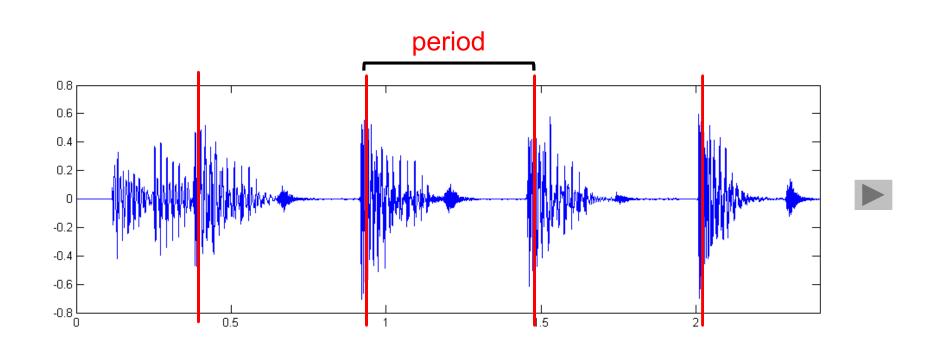


Tasks

- Onset detection
- Beat tracking
- Tempo estimation

Tempo := 60 / period

Beats per minute (BPM)

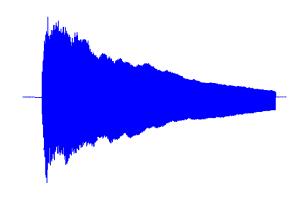


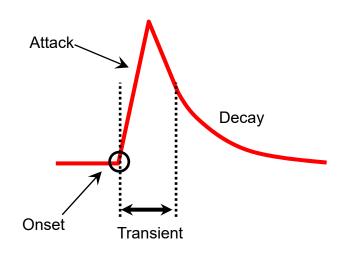
Onset Detection

- Finding start times of perceptually relevant acoustic events in music signal
- Onset is the time position where a note is played
- Onset typically goes along with a change of the signal's properties:
 - energy or loudness
 - pitch or harmony
 - timbre

Onset Detection

- Finding start times of perceptually relevant acoustic events in music signal
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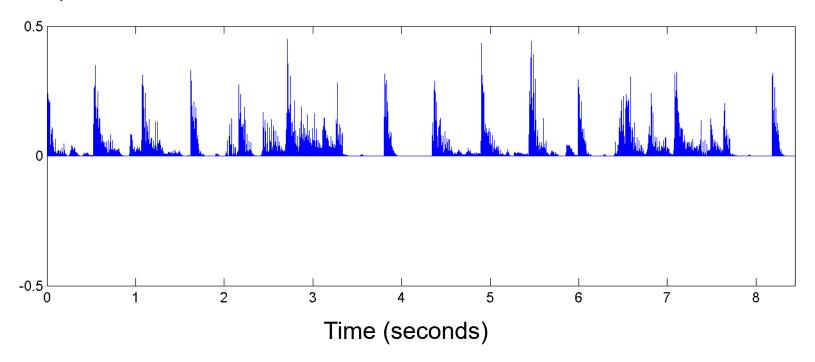


0.8 0.6 0.4 0.2 0.4 0.2 0.4 0.6 0.8 0.6 0.7 Time (seconds)

Steps

1. Amplitude squaring

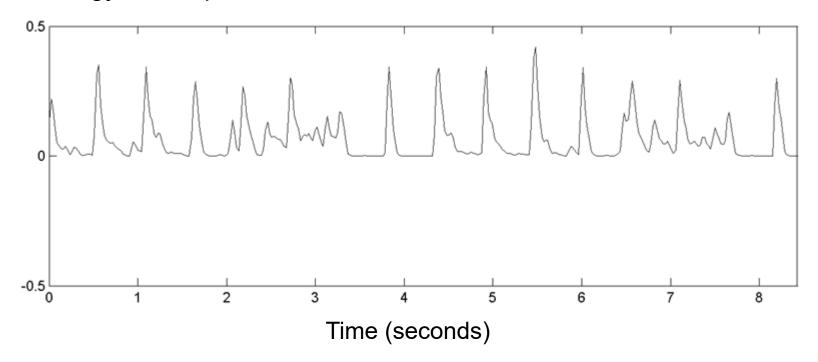
Squared waveform



Steps

- 1. Amplitude squaring
- 2. Windowing

Energy envelope

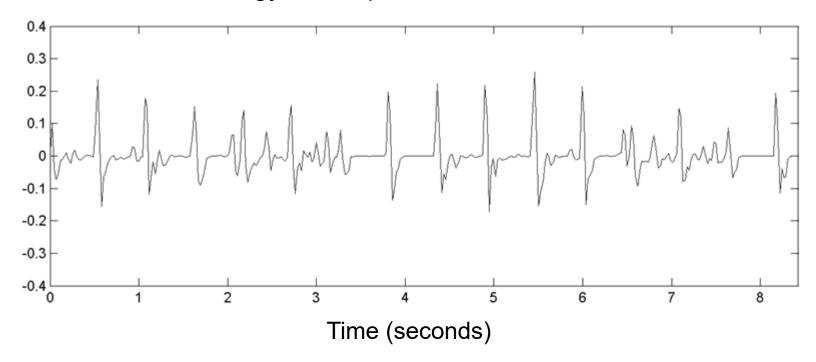


Steps

- 1. Amplitude squaring
- 2. Windowing
- 3. Differentiation

Capturing energy changes

Differentiated energy envelope

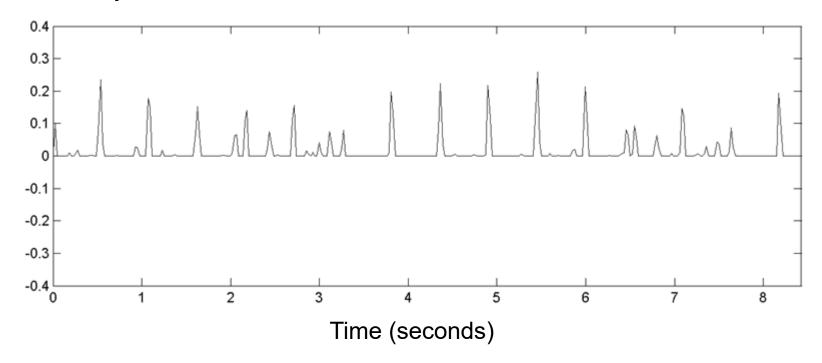


Steps

- 1. Amplitude squaring
- 2. Windowing
- 3. Differentiation
- 4. Half wave rectification

Only energy increases are relevant for note onsets

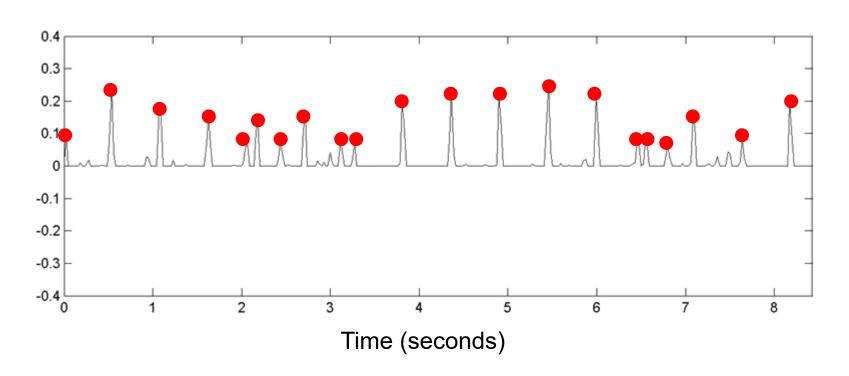
Novelty curve



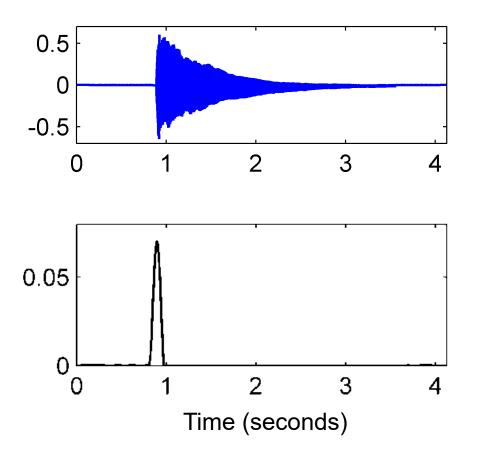
Steps

- 1. Amplitude squaring
- 2. Windowing
- 3. Differentiation
- 4. Half wave rectification
- 5. Peak picking

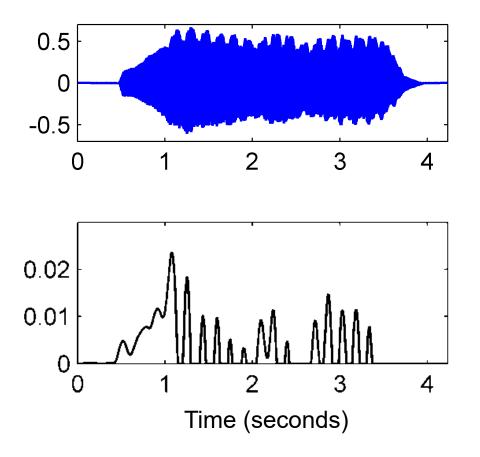
Peak positions indicate note onset candidates



Example: C4 played by piano



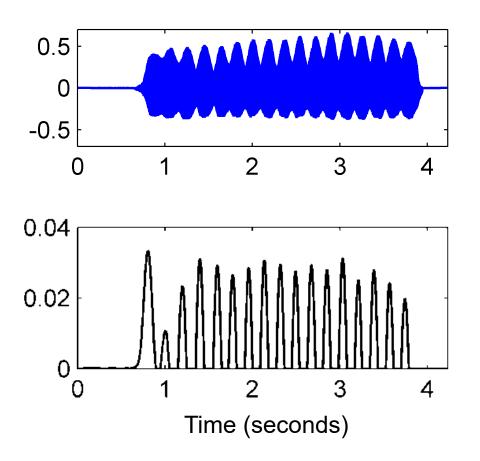
Example: C4 played by violin







Example: C4 played by flute

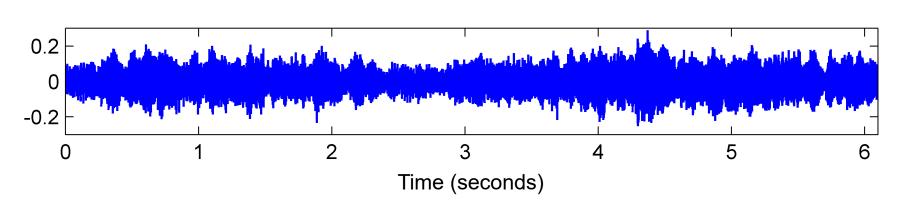


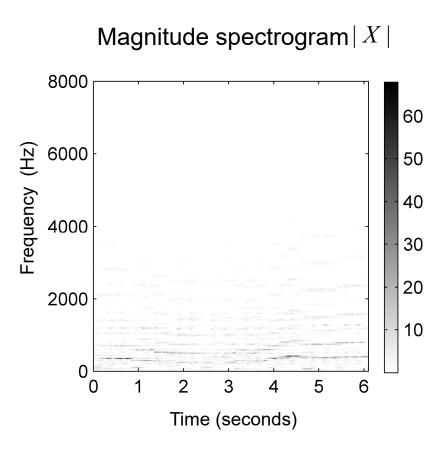
Onset Detection

- Energy curves often only work for percussive music
- Many instruments such as strings have weak note onsets
- No energy increase may be observable in complex sound mixtures
- More refined methods needed that capture
 - changes of spectral content
 - changes of pitch
 - changes of harmony



Audio recording

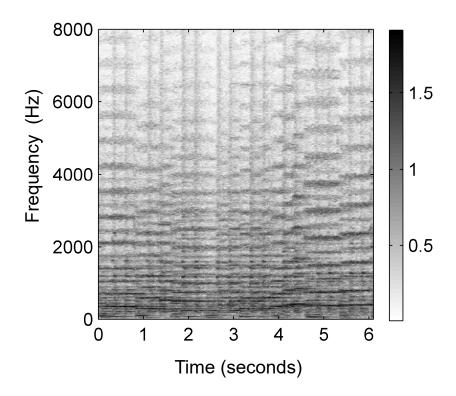




Steps:

1. Spectrogram

Compressed spectrogram Y

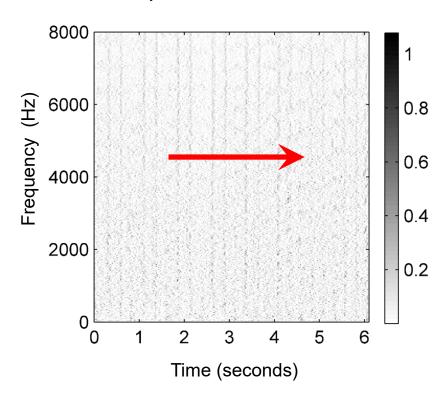


Steps:

- 1. Spectrogram
- 2. Logarithmic compression

$$Y = \log(1 + C \cdot |X|)$$

Spectral difference



Steps:

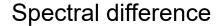
- 1. Spectrogram
- 2. Logarithmic compression
- Differentiation & half wave rectification

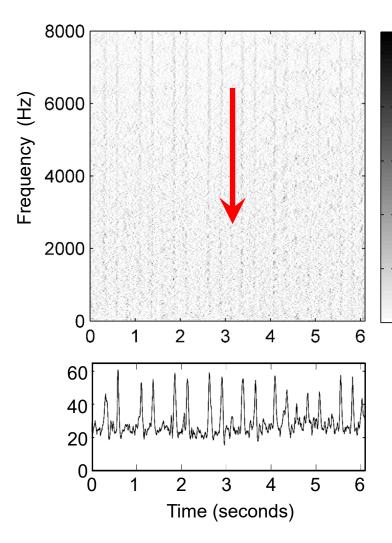
8.0

0.6

0.4

0.2





Steps:

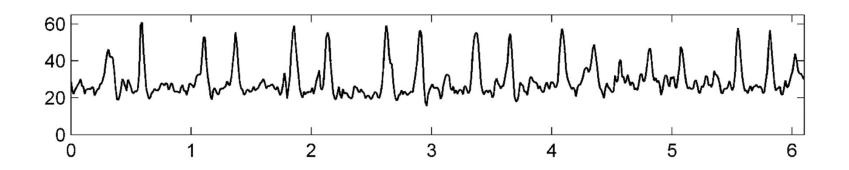
- 1. Spectrogram
- 2. Logarithmic compression
- 3. Differentiation & half wave rectification
- 4. Accumulation

Novelty curve

Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- 3. Differentiation & half wave rectification
- 4. Accumulation

Novelty curve

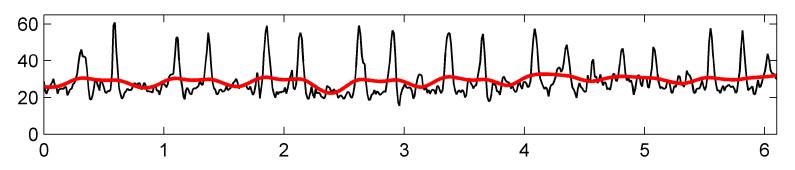


Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- 3. Differentiation & half wave rectification
- 4. Accumulation
- 5. Normalization

Novelty curve

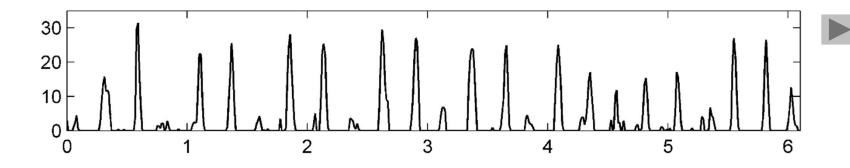
Substraction of local average



Steps:

- 1. Spectrogram
- 2. Logarithmic compression
- 3. Differentiation & half wave rectification
- 4. Accumulation
- 5. Normalization

Normalized novelty curve



$$t \in [1:T]$$

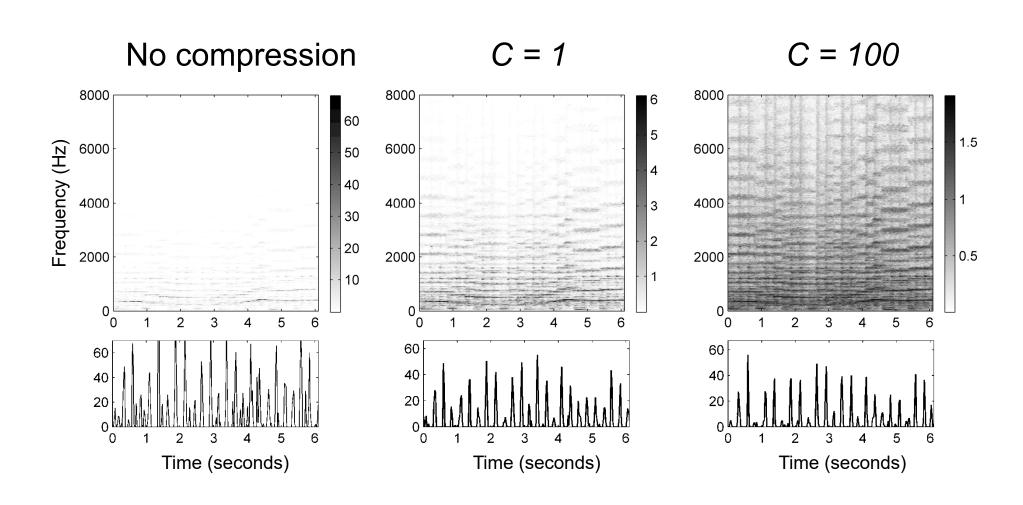
• Spectrogram $X = (X(t,k))_{t,k}$

- $k \in [1:K]$
- Compressed Spectrogram $Y := \log(1 + C \cdot |X|)$ C > 1
- Novelty curve $\Delta: [1:T-1] \to \mathbb{R}$:

$$\Delta(t) := \sum_{k=1}^{K} |Y(t+1,k) - Y(t,k)|_{\geq 0}$$

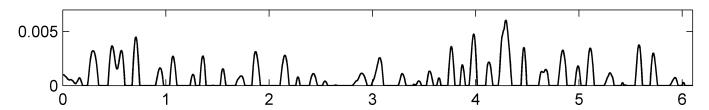
Logarithmic Compression

$$Y = \log(1 + C \cdot |X|)$$

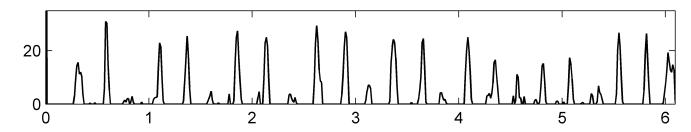


Onset Detection

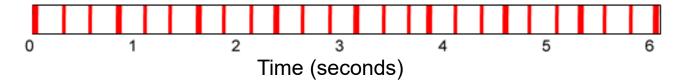
Energy-based novelty curve



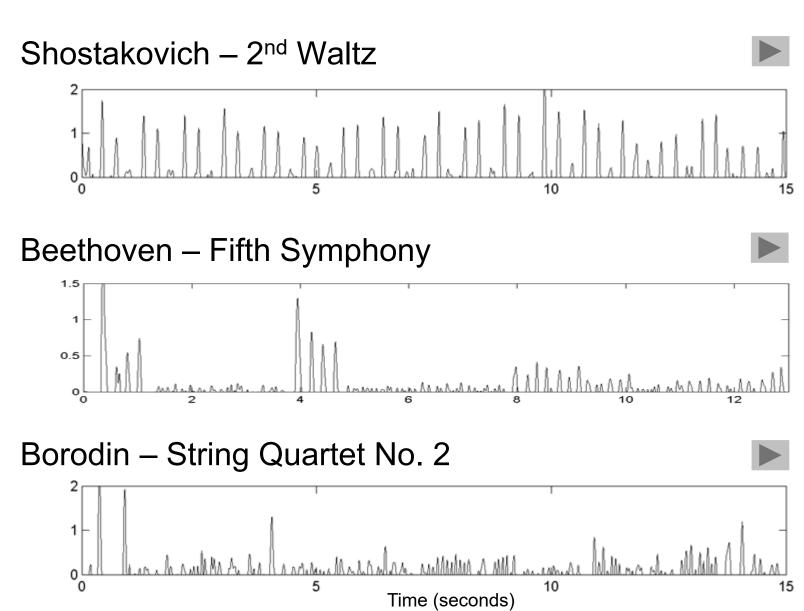
Spectral-based novelty curve



Manuel onset annotations



Onset Detection



Onset Detection

Drumbeat

Going Home

Lyphard melodie

Por una cabeza

Donau



Beat and Tempo

What is a beat?

- Steady pulse that drives music forward and provides the temporal framework of a piece of music
- Sequence of perceived pulses that are equally spaced in time
- The pulse a human taps along when listening to the music

[Parncutt 1994]

[Sethares 2007]

[Large/Palmer 2002]

[Lerdahl/ Jackendoff 1983]

[Fitch/ Rosenfeld 2007]

The term tempo then refers to the speed of the pulse.

Beat and Tempo

Strategy

- Analyze the novelty curve with respect to reoccurring or quasiperiodic patterns
- Avoid the explicit determination of note onsets (no peak picking)

Beat and Tempo

Strategy

- Analyze the novelty curve with respect to reoccurring or quasiperiodic patterns
- Avoid the explicit determination of note onsets (no peak picking)

[Scheirer, JASA 1998]

Methods

[Ellis, JNMR 2007]

Comb-filter methods

[Davies/Plumbley, IEEE-TASLP 2007]

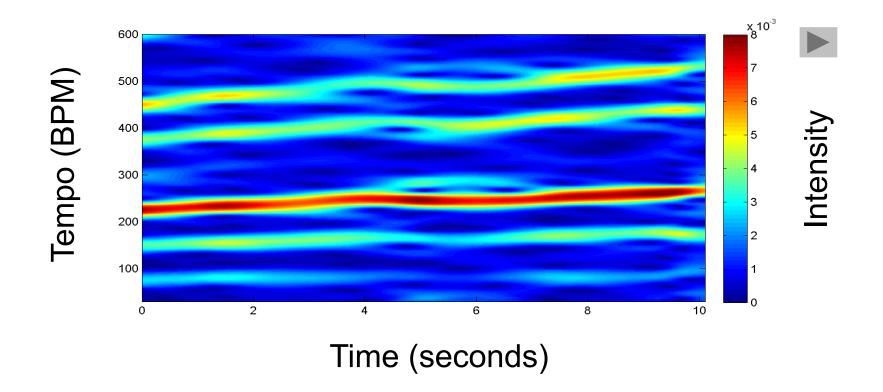
Autocorrelation

[Peeters, JASP 2007]

Fourier transfrom

[Grosche/Müller, ISMIR 2009] [Grosche/Müller, IEEE-TASLP 2011]

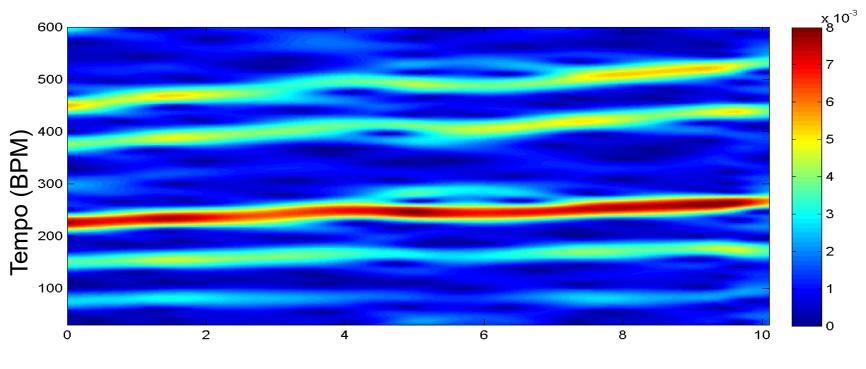
Definition: A tempogram is a time-tempo representation that encodes the local tempo of a music signal over time.



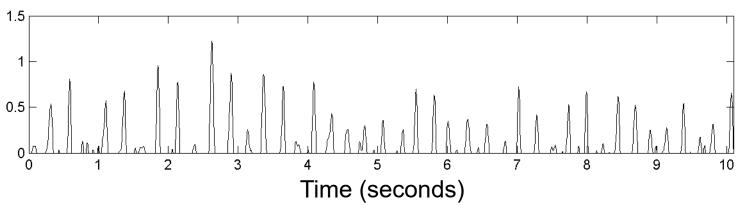
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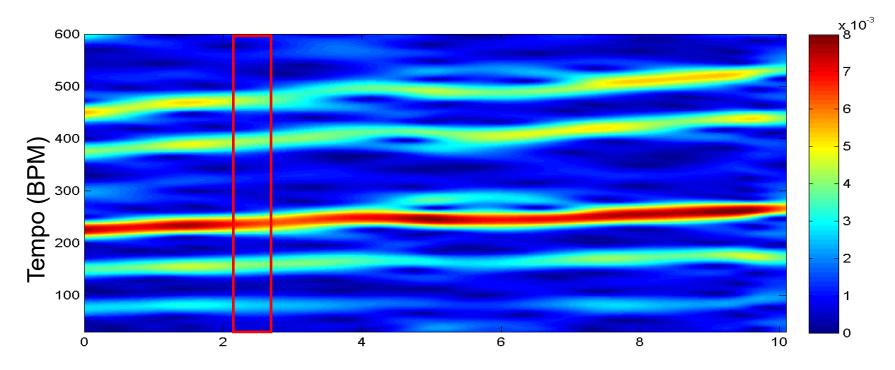
Fourier-based method

- Compute a spectrogram (STFT) of the novelty curve
- Convert frequency axis (given in Hertz) into tempo axis (given in BPM)
- Magnitude spectrogram indicates local tempo

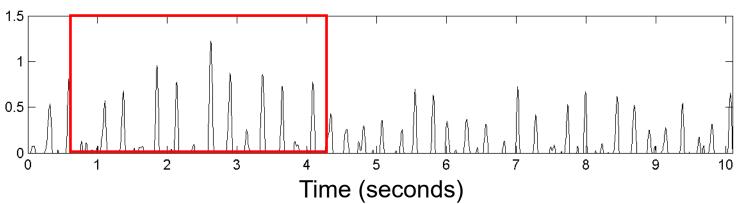


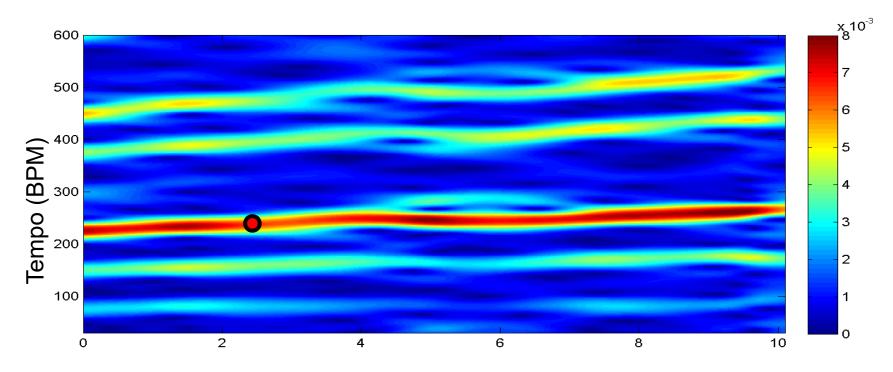
Novelty curve



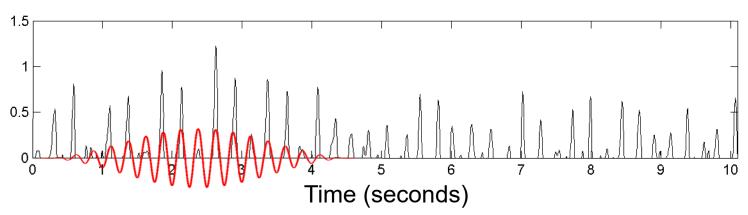


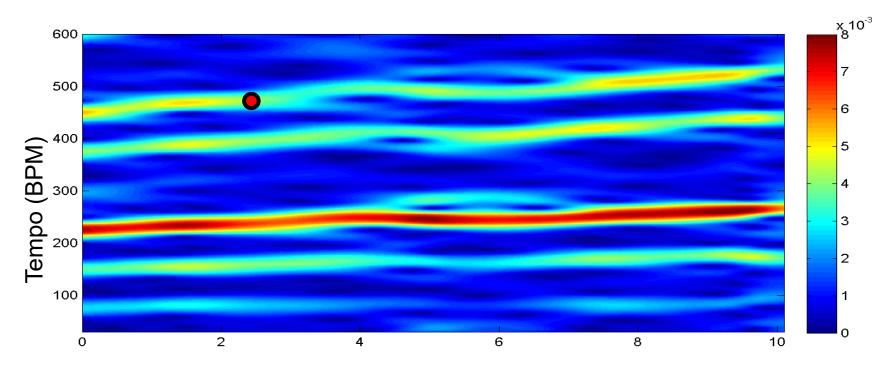
Novelty curve (local section)



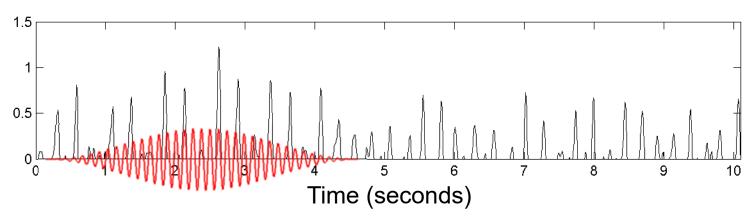


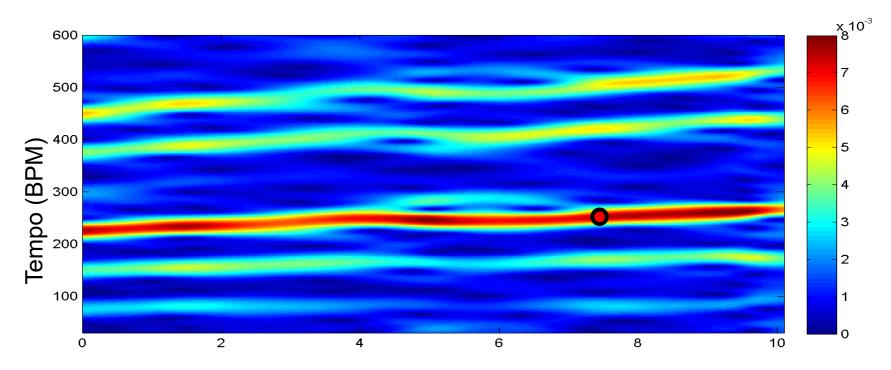
Windowed sinusoidal



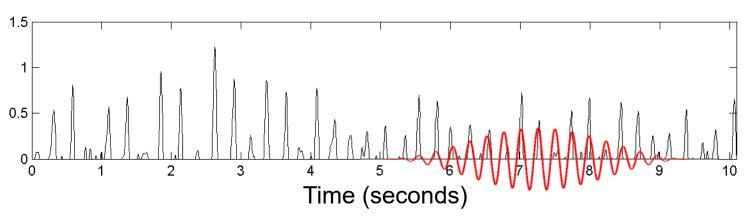


Windowed sinusoidal





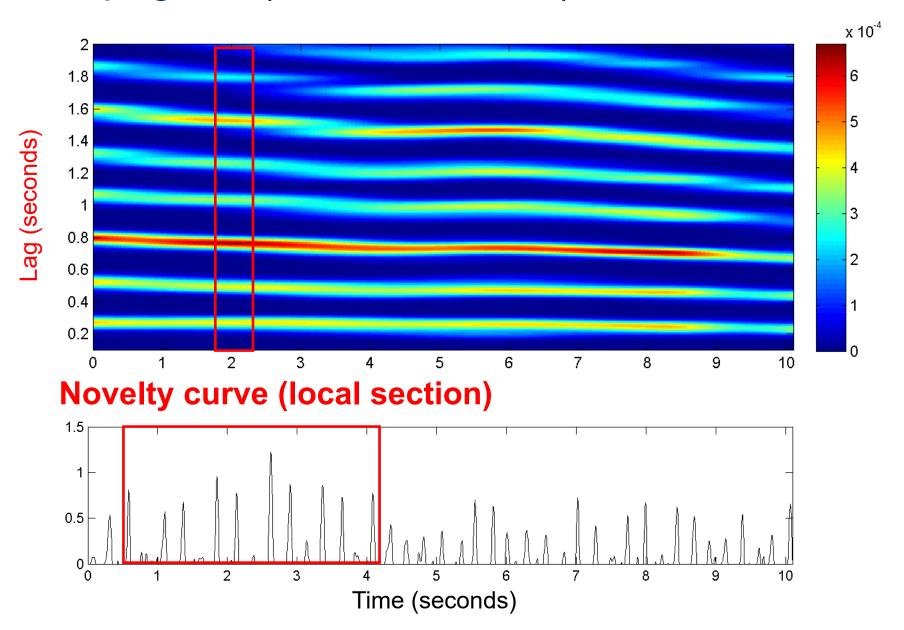
Windowed sinusoidal

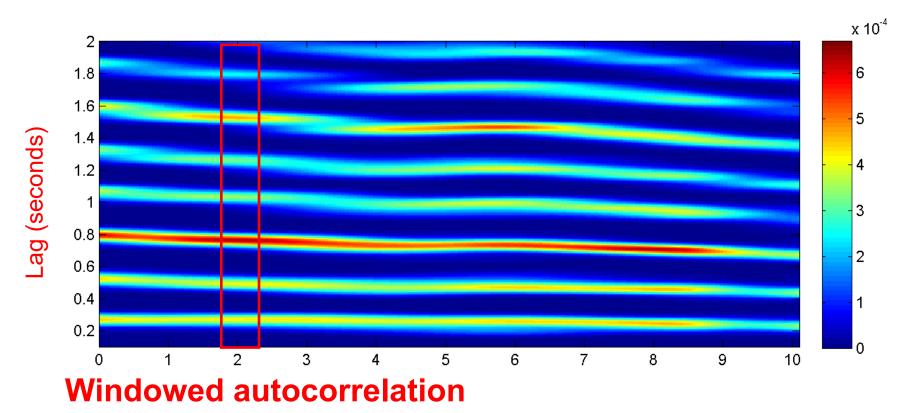


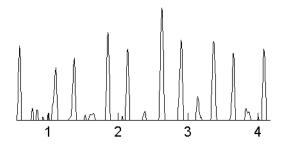
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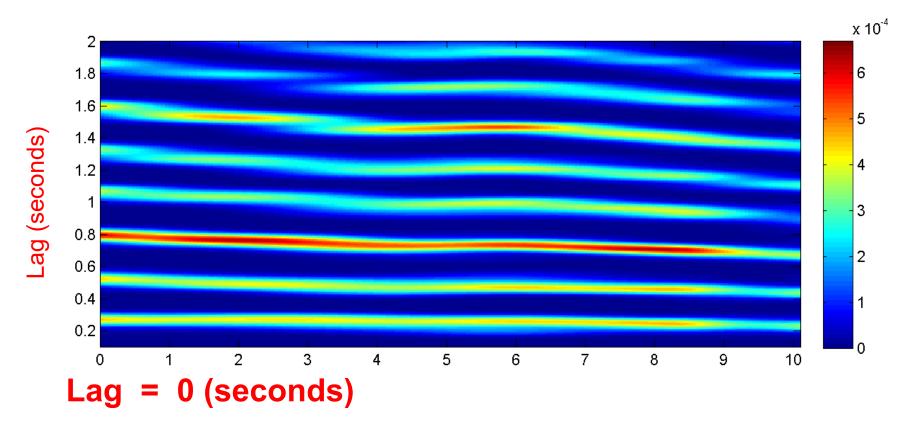
Autocorrelation-based method

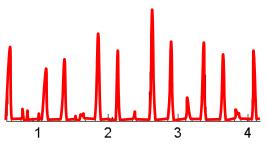
- Compare novelty curve with time-lagged local sections of itself
- Convert lag-axis (given in seconds) into tempo axis (given in BPM)
- Autocorrelogram indicates local tempo

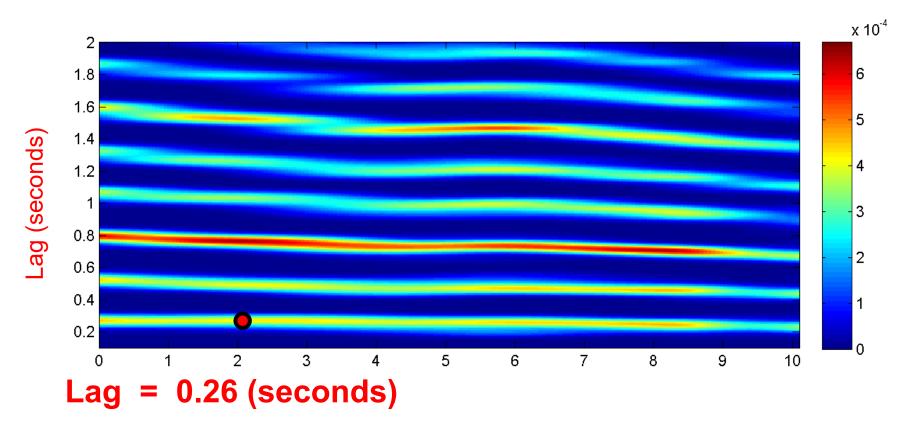


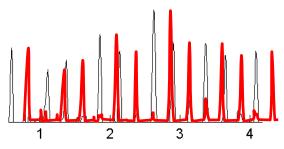


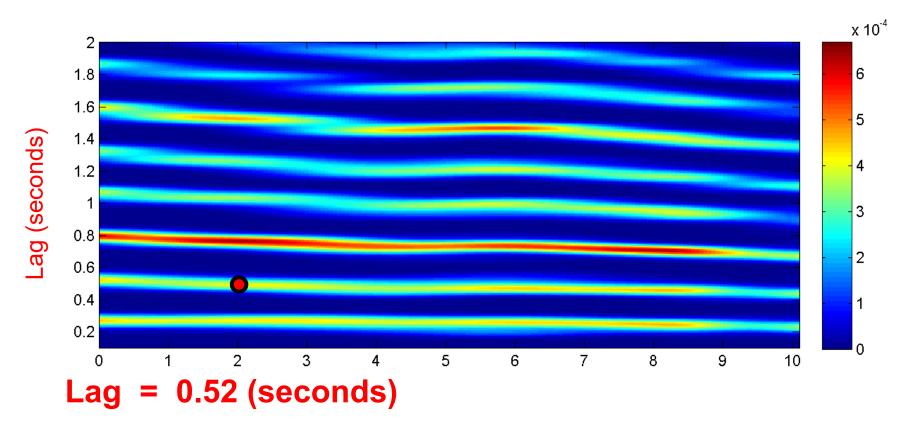


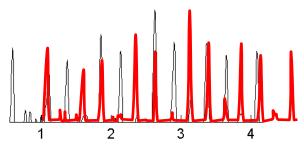


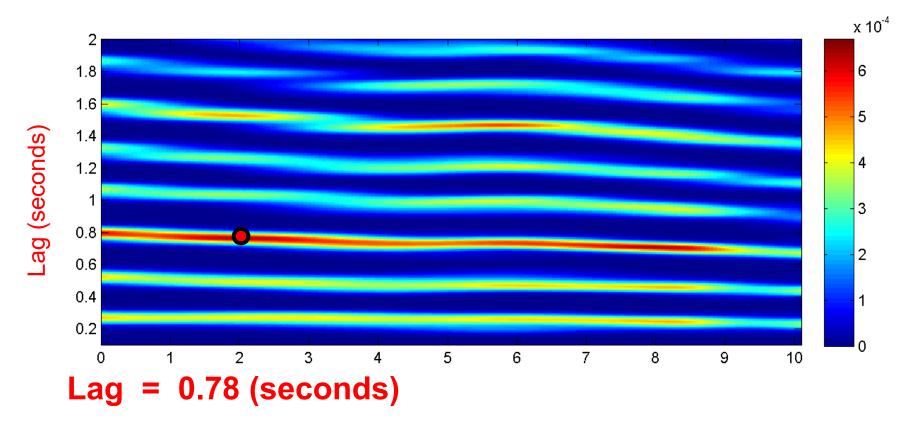


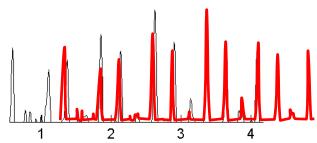


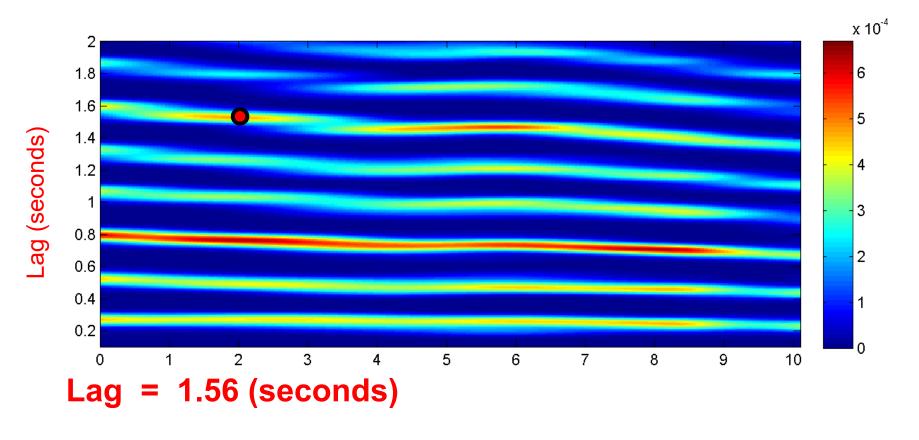


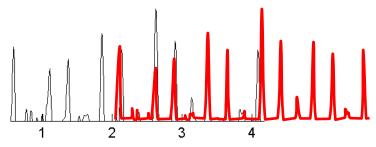


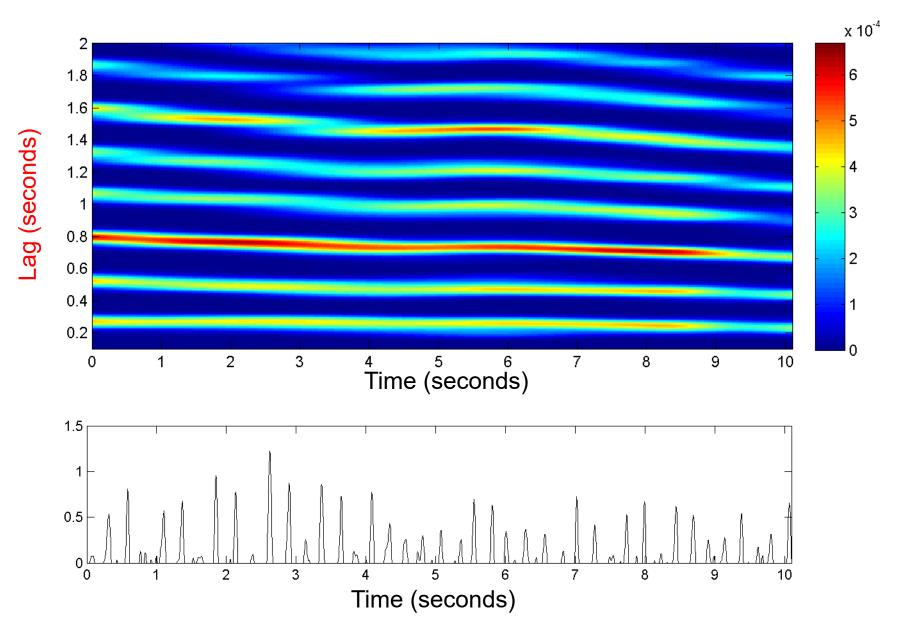


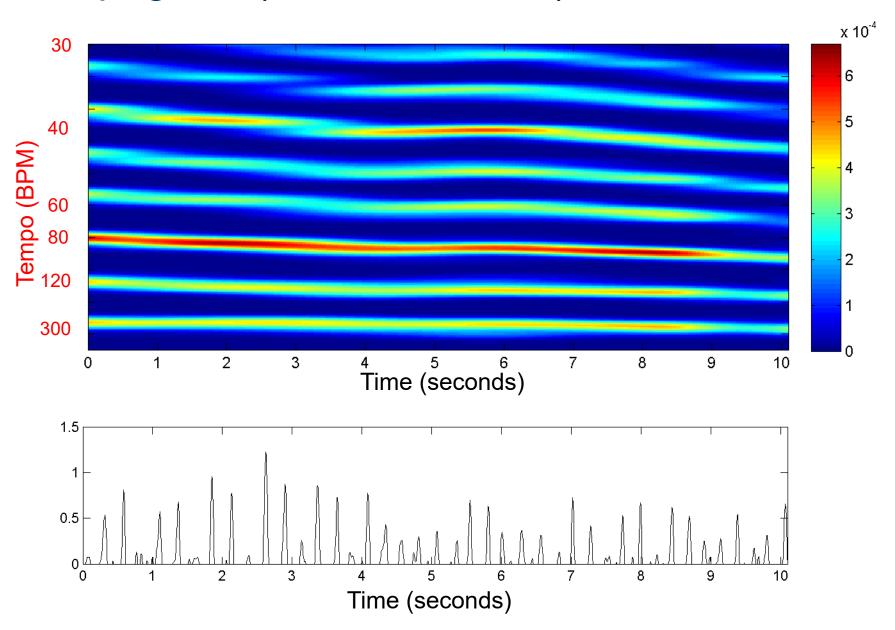


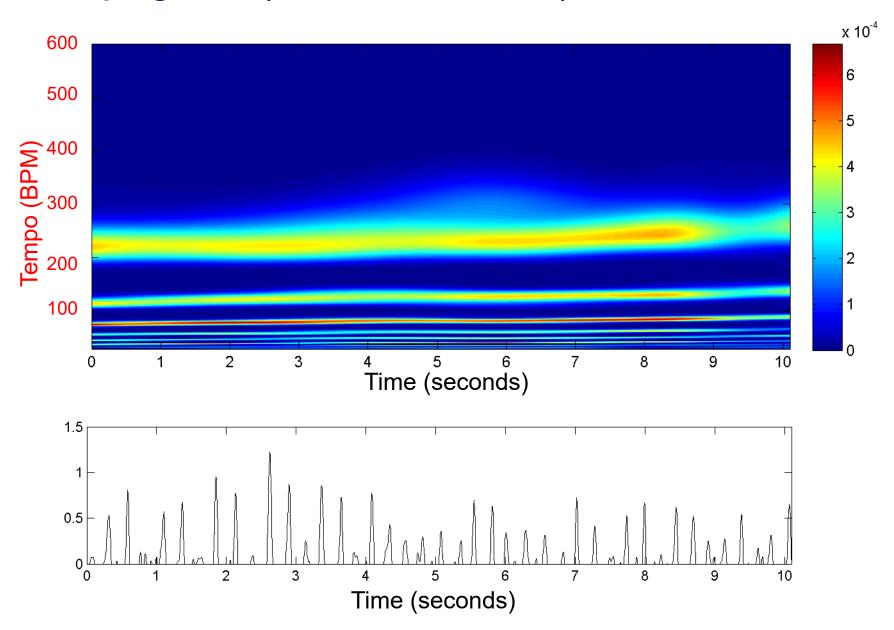


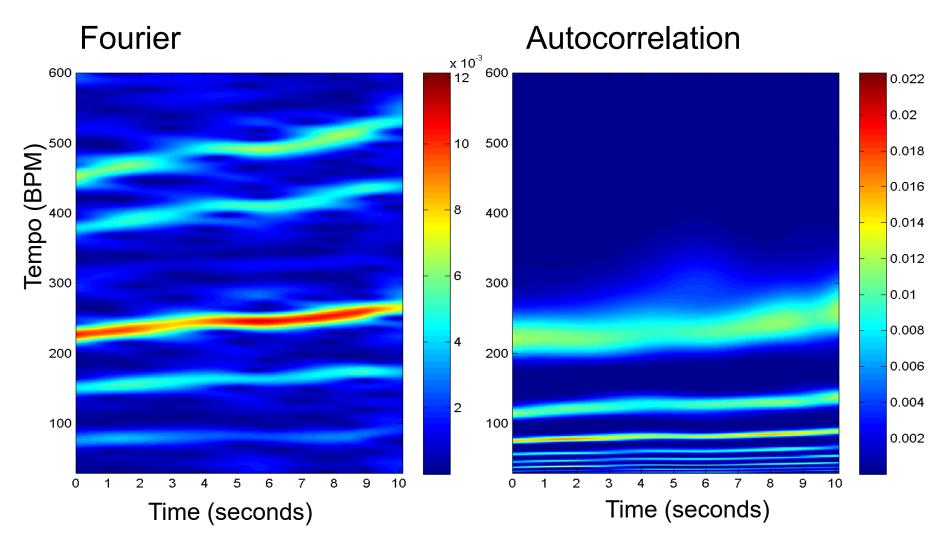


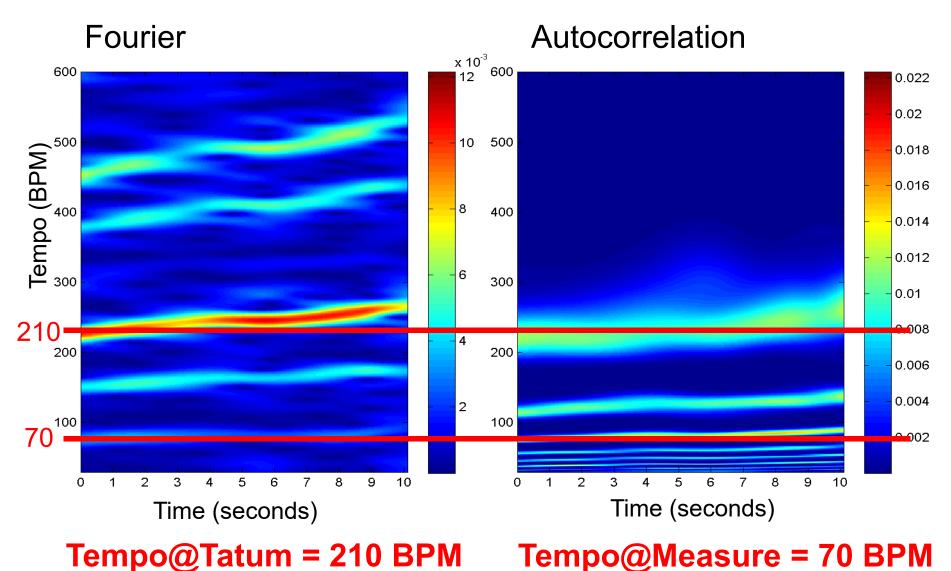


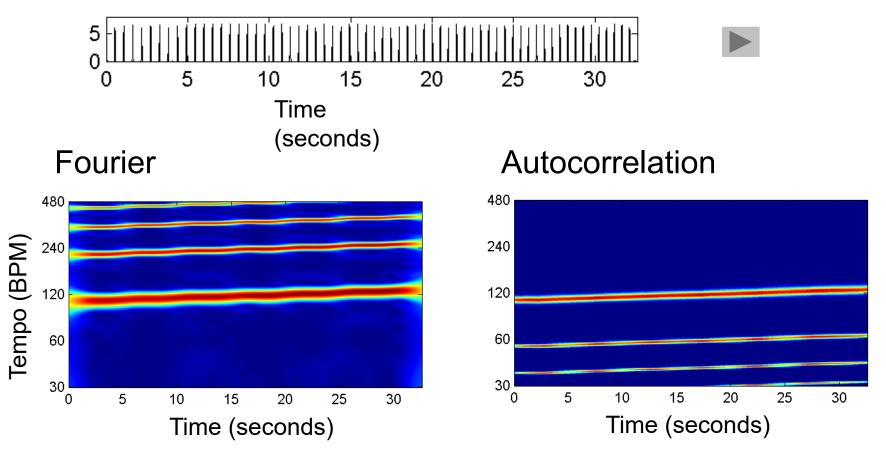












Emphasis of tempo harmonics (integer multiples)

Emphasis of tempo subharmonics (integer fractions)

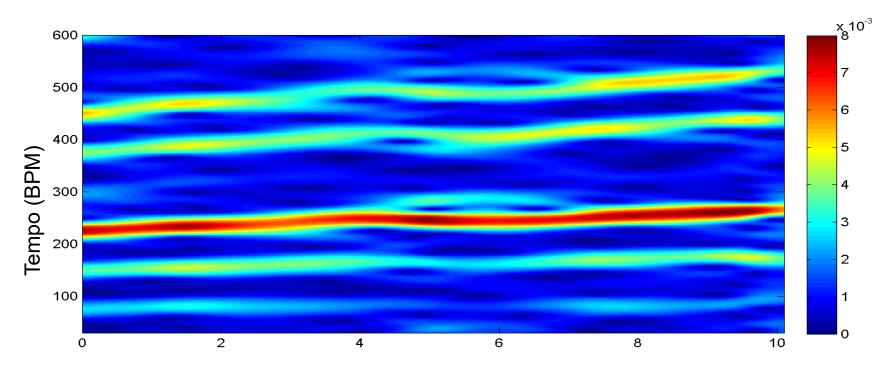
Tempogram (Summary)

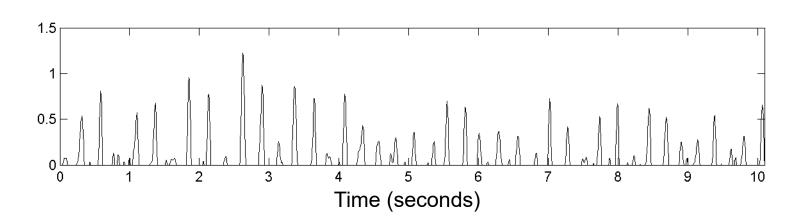
Fourier	Autocorrelation
Novelty curve is compared with sinusoidal kernels each representing a specific tempo	Novelty curve is compared with time-lagged local (windowed) sections of itself
Convert frequency (Hertz) into tempo (BPM)	Convert time-lag (seconds) into tempo (BPM)
Reveals novelty periodicities	Reveals novelty self-similarities
Emphasizes harmonics	Emphasizes subharmonics
Suitable to analyze tempo on tatum and tactus level	Suitable to analyze tempo on tactus and measure level

Beat Tracking

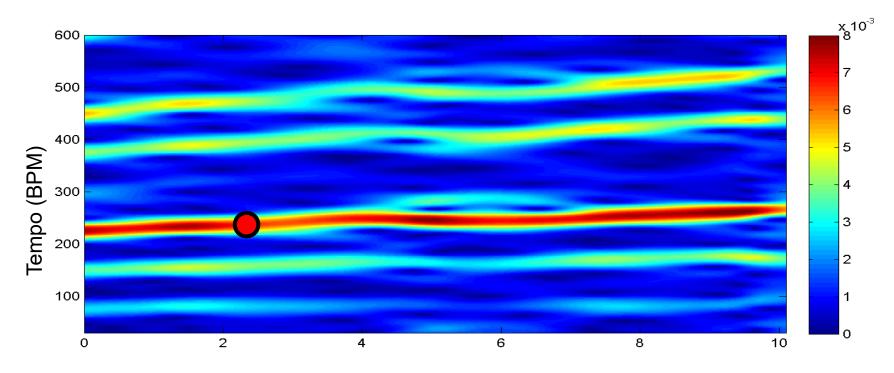
- Given the tempo, find the best sequence of beats
- Complex Fourier tempogram contains magnitude and phase information
- The magnitude encodes how well the novelty curve resonates with a sinusoidal kernel of a specific tempo
- The phase optimally aligns the sinusoidal kernel with the peaks of the novelty curve

Local Pulse Tracking

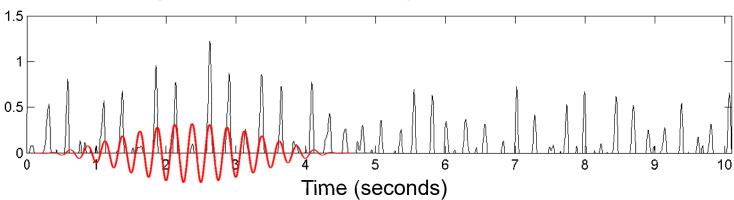


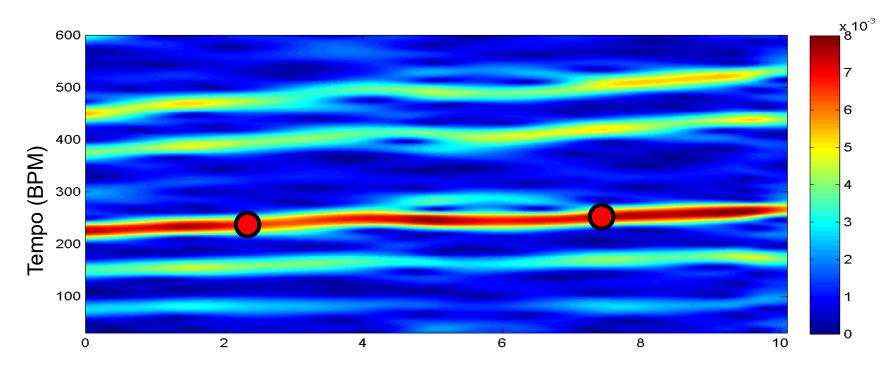


Local Pulse Tracking

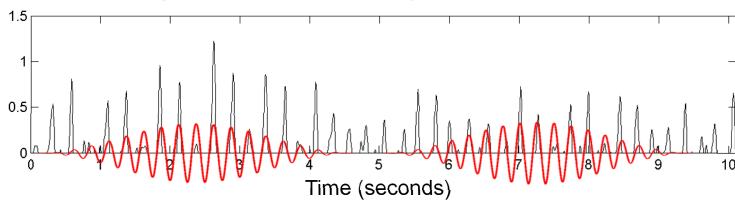


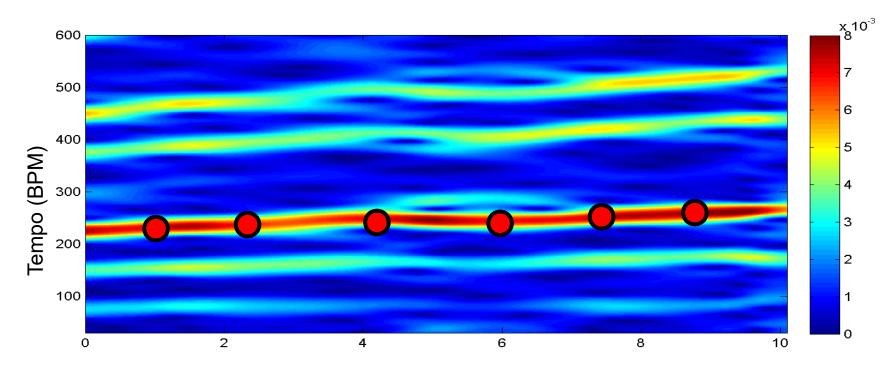
Optimizing local periodicity kernel



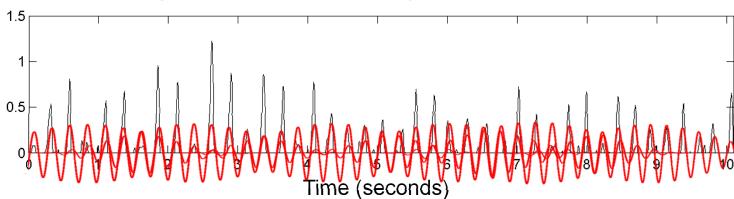


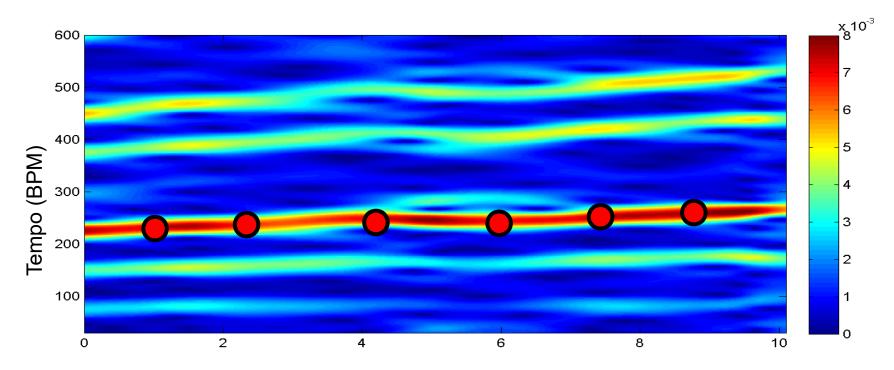
Optimizing local periodicity kernel



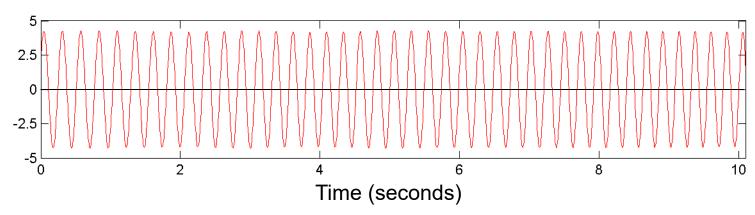


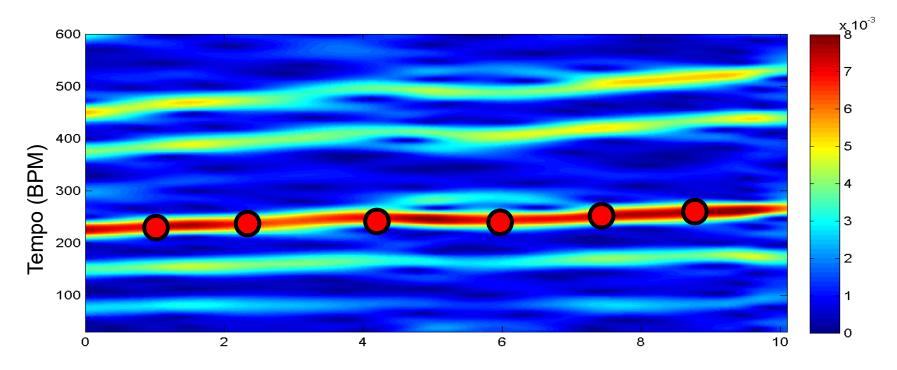
Optimizing local periodicity kernel



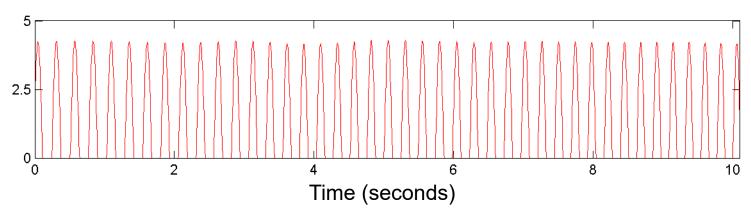


Accumulation of kernels

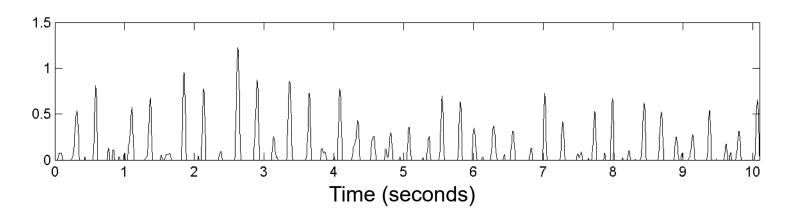




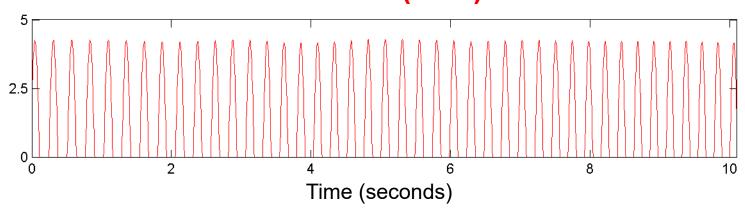
Halfwave rectification



Novelty Curve



Predominant Local Pulse (PLP)



Novelty Curve

- Indicates note onset candidates
- Extraction errors in particular for soft onsets
- Simple peak-picking problematic

Predominant Local Pulse (PLP)

- Periodicity enhancement of novelty curve
- Accumulation introduces error robustness
- Locality of kernels handles tempo variations

• Local tempo at time t : $au_t \in \Theta$

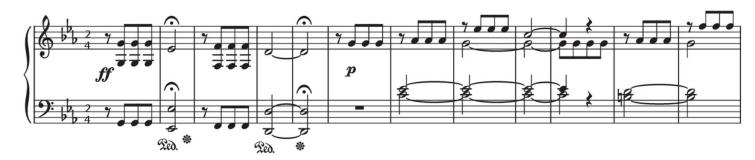
 $\Theta = [60:240]$ BPM

- Phase $\varphi_t := \frac{1}{2\pi} \arccos\left(\frac{\operatorname{Re}(\mathcal{T}(t, \tau_t))}{|\mathcal{T}(t, \tau_t)|}\right)$
- Sinusoidal kernel $\kappa_t: \mathbb{Z} \to \mathbb{R}$

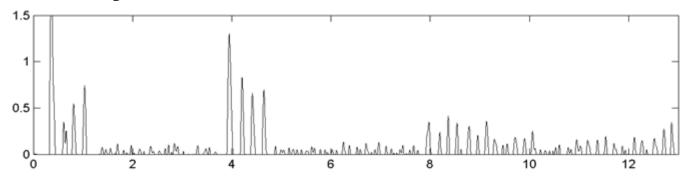
$$\kappa_t(n) := W(n-t)\cos(2\pi(\tau_t/60 \cdot n - \varphi_t))$$
 $n \in \mathbb{Z}$

• Periodicity curve $\Gamma: [1:T] \to \mathbb{R}_{\geq 0}$

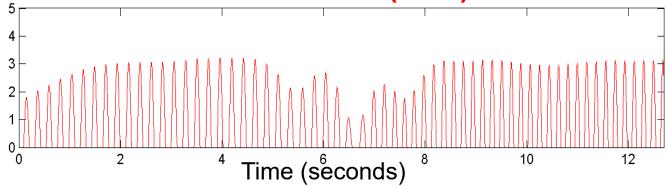
$$\Gamma(n) = \left| \sum_{t \in [1:T]} \kappa_t(n) \right|_{\geq 0} \qquad n \in [1:T]$$



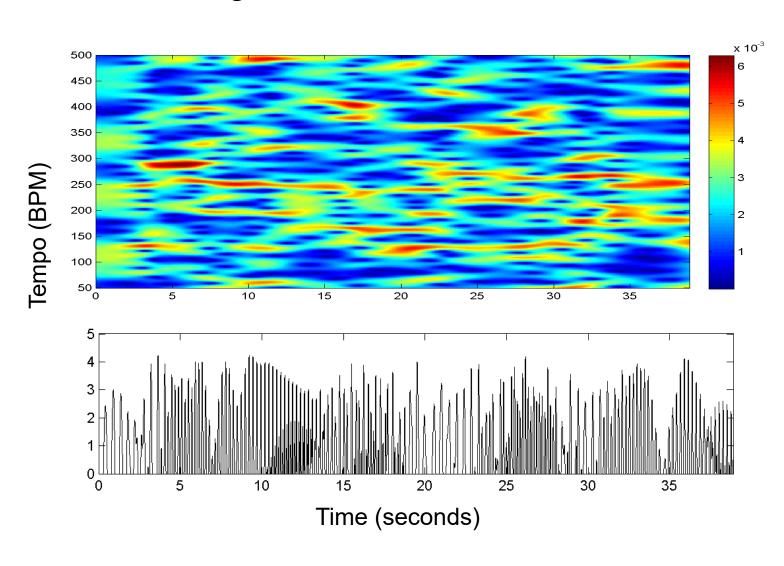
Novelty Curve



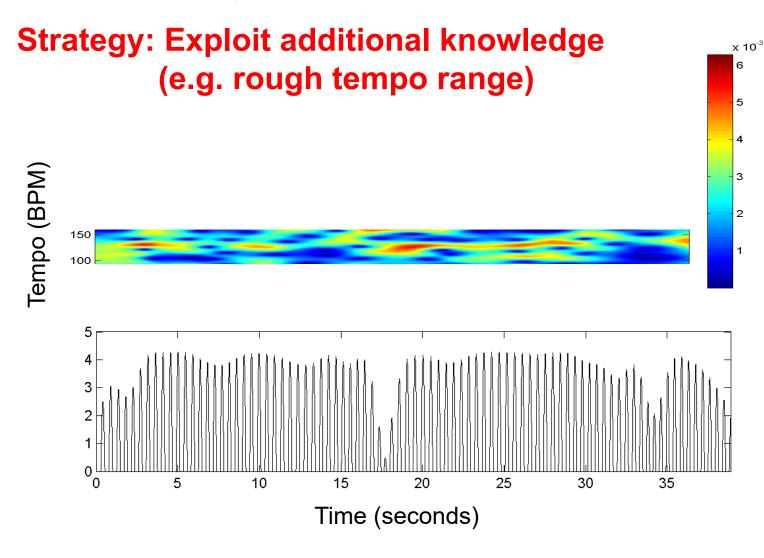
Predominant Local Pulse (PLP)



Borodin – String Quartet No. 2

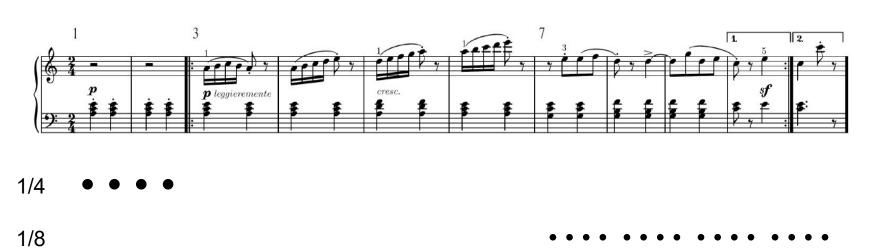


Borodin – String Quartet No. 2



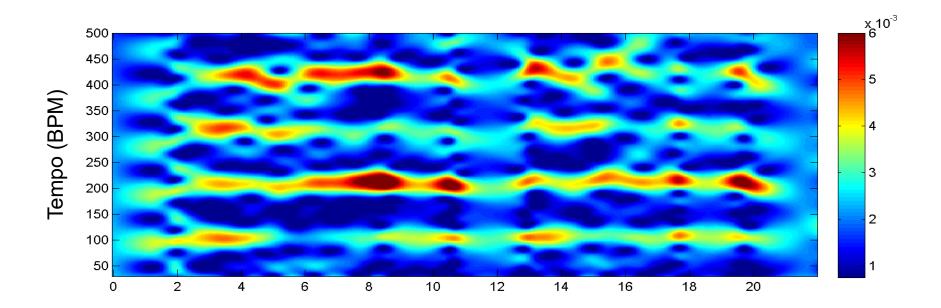
Piano Etude Op. 100 No. 2 by Burgmüller

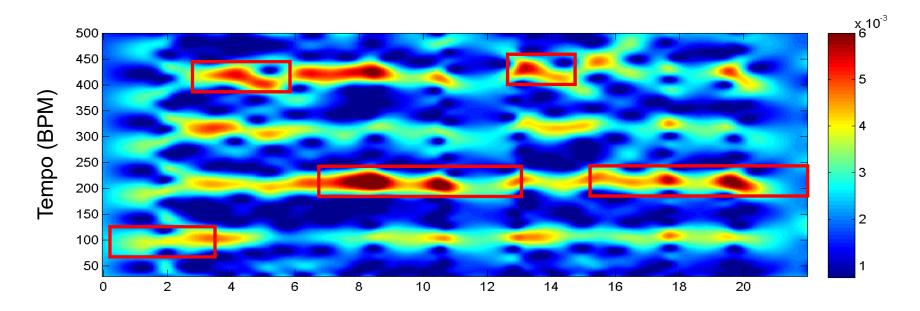




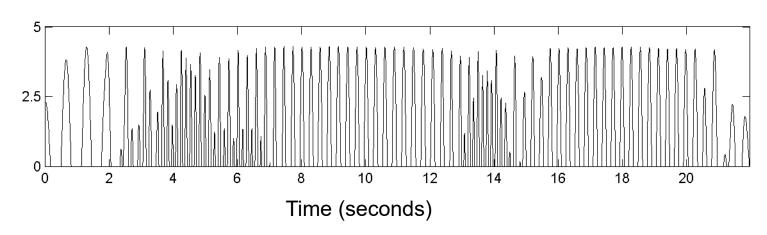
1/16

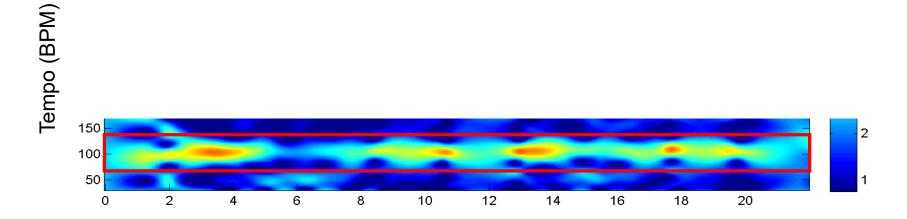
What is the pulse level: Measure – Tactus – Tatum?



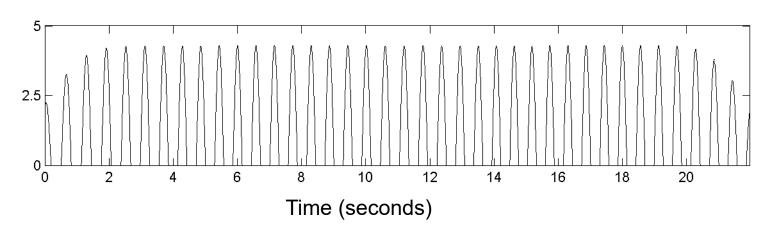


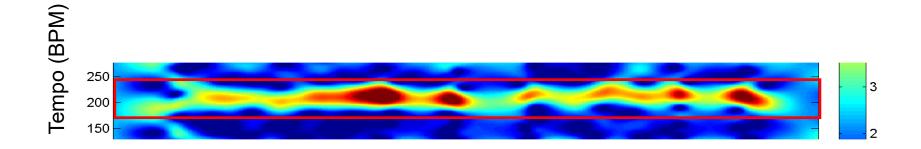
Switching of predominant pulse level



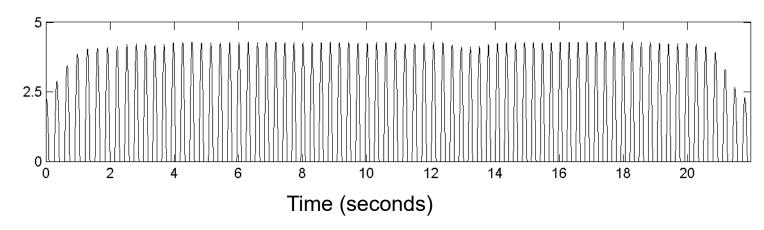


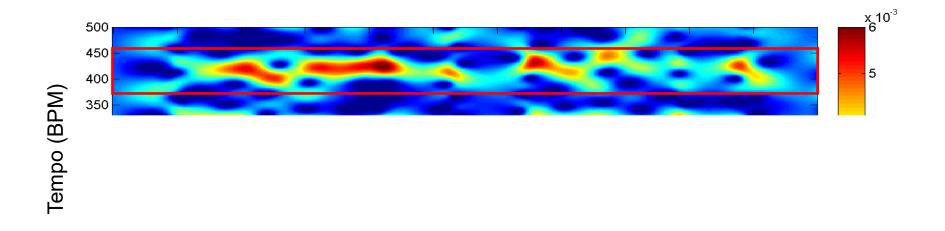
1/4 note pulse level



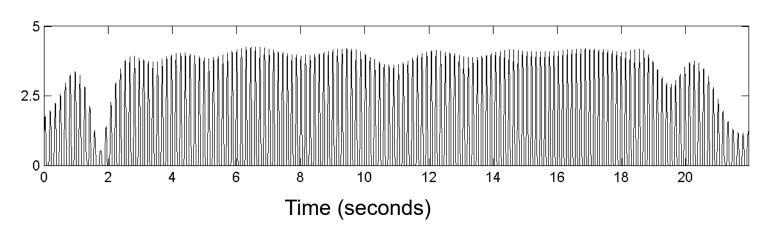


1/8 note pulse level



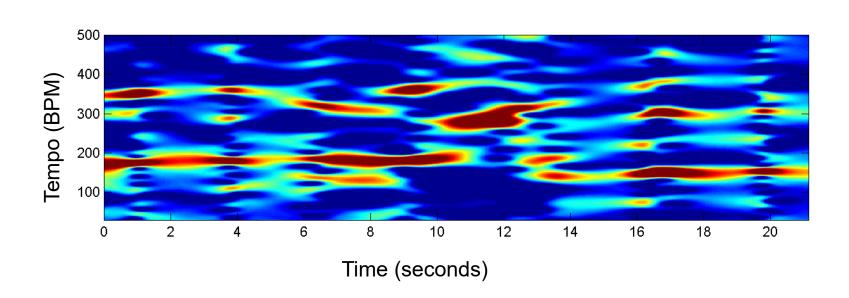


1/16 note pulse level

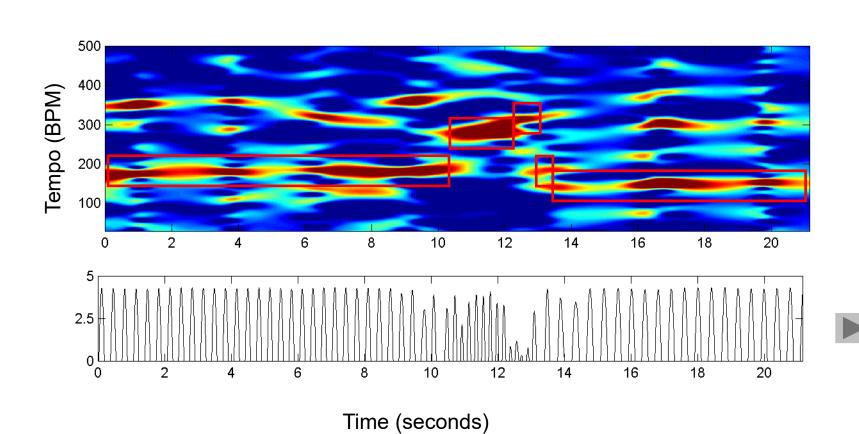


Brahms Hungarian Dance No. 5





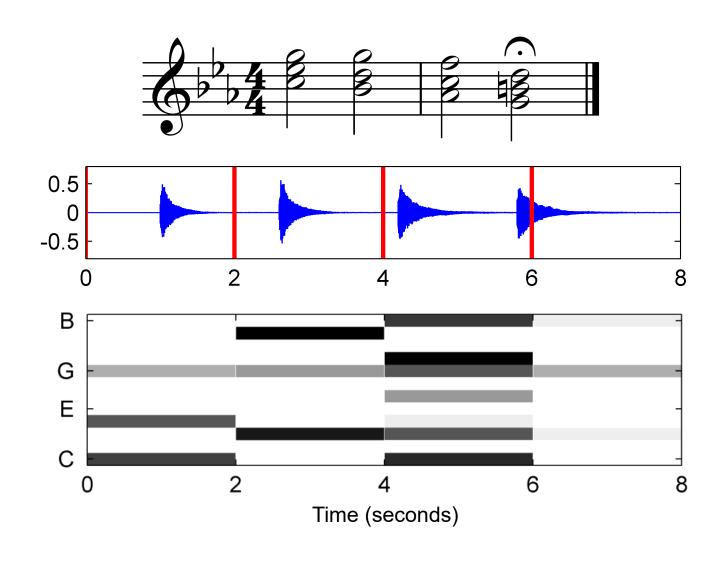
Brahms Hungarian Dance No. 5



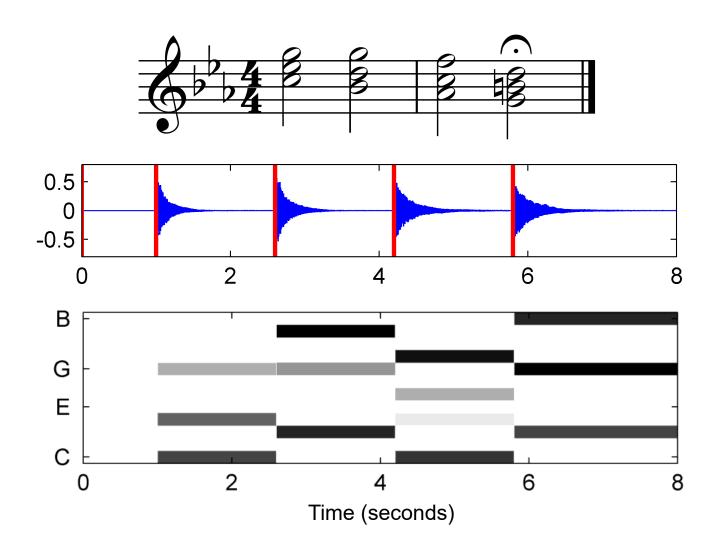
Applications

- Feature design (beat-synchronous features, adaptive windowing)
- Digital DJ / audio editing (mixing and blending of audio material)
- Music classification
- Music recommendation
- Performance analysis (extraction of tempo curves)

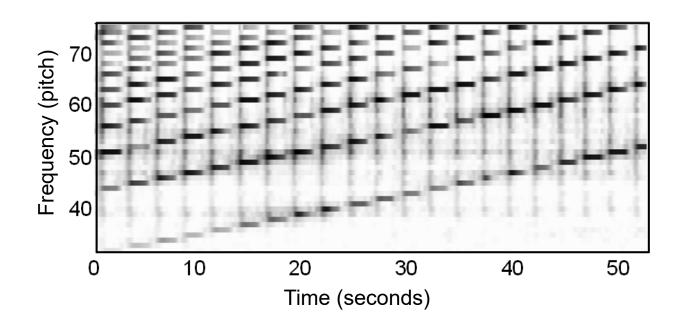
Fixed window size



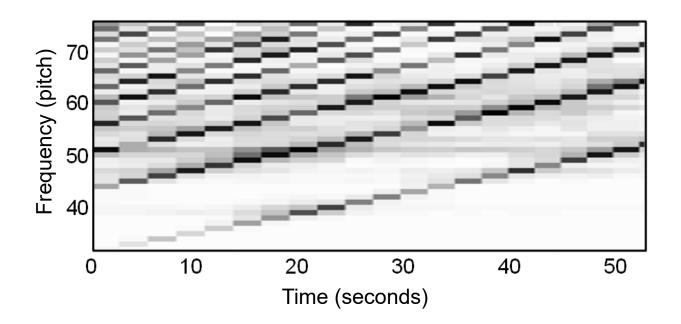
Adaptive window size



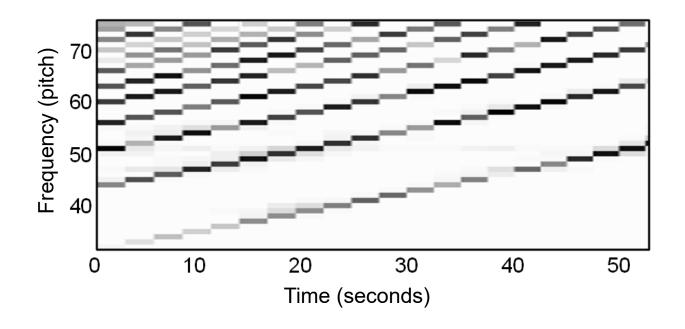
Fixed window size



Adaptive window size



Adaptive window size

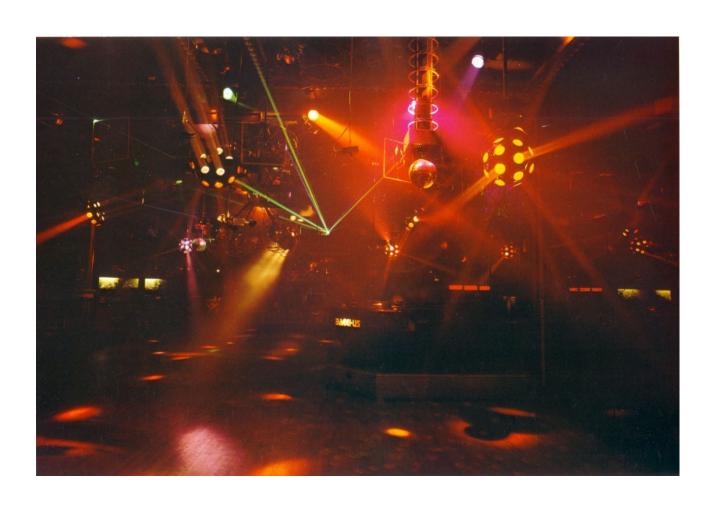


Denoising by excluding boundary neighborhoods

Application: Audio Editing (Digital DJ)



Application: Beat-Synchronous Light Effects



Summary

1. Onset Detection

- Novelty curve (something is changing)
- Indicates note onset candidates
- Hard task for non-percussive instruments (strings)

2. Tempo Estimation

- Fourier tempogram
- Autocorrelation tempogram
- Musical knowledge (tempo range, continuity)

3. Beat tracking

- Find most likely beat positions
- Exploiting phase information from Fourier tempogram